

# THE Attenuation Characteristic In Arc-continent Collision Zone Of Taiwan From Shallow To Deep

王郁如

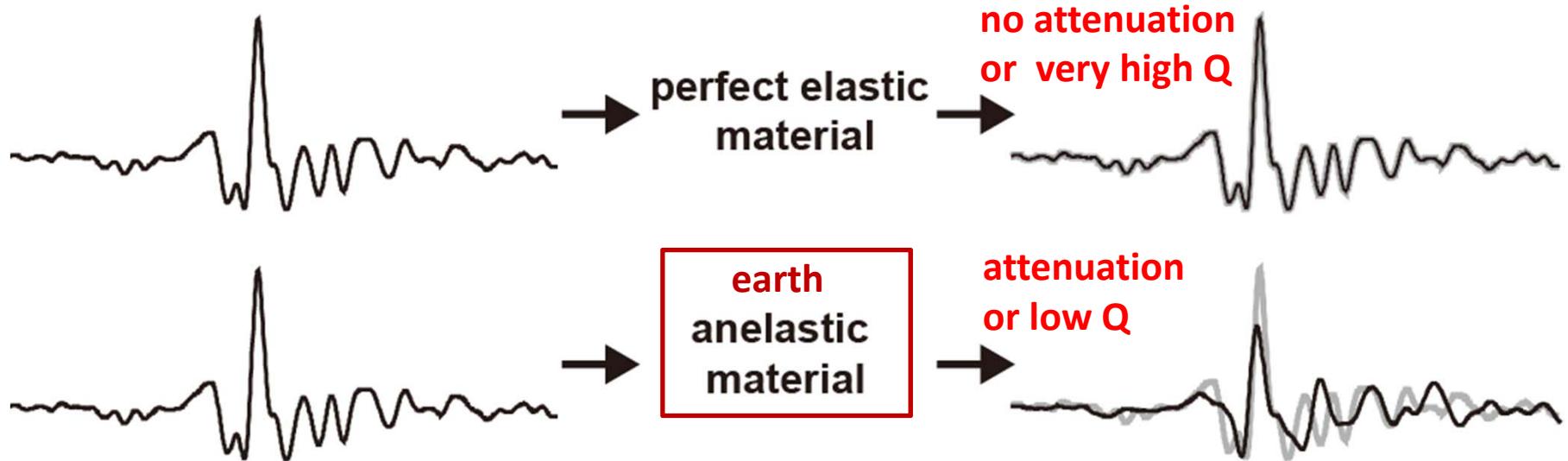
Yu-Ju Wang

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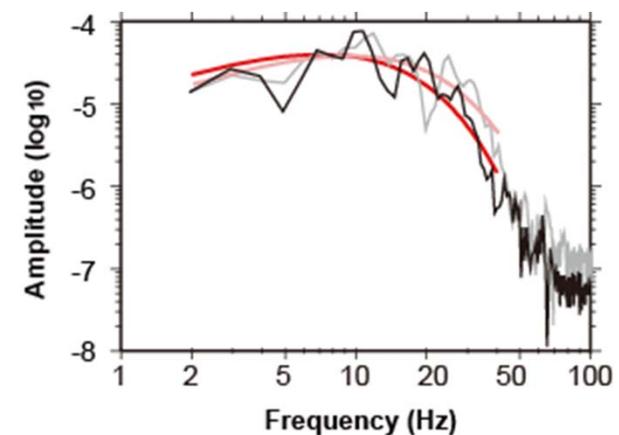
# outlines

- \* **Introduction : Attenuation ( $Q^{-1}$ )**
- \* **The attenuation properties of the Taiwan orogenic structure**
- \* **The attenuation features within the Chelungpu fault zone**
- \* **The subsurface attenuation model of Taiwan (depth ~300 m)**
- \* **New Attenuation Relationship for normal faulting earthquakes in the northeast offshore Taiwan**

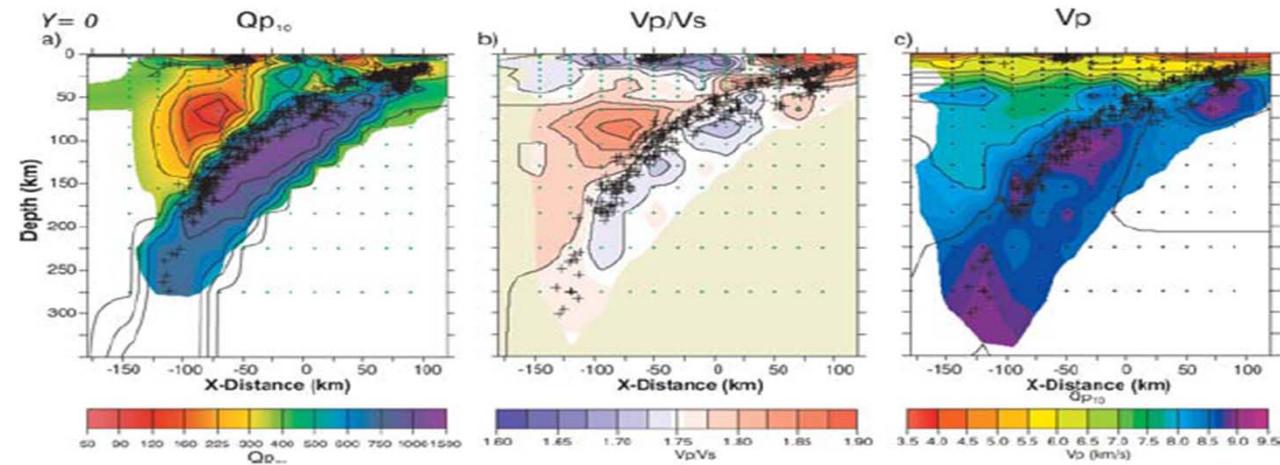
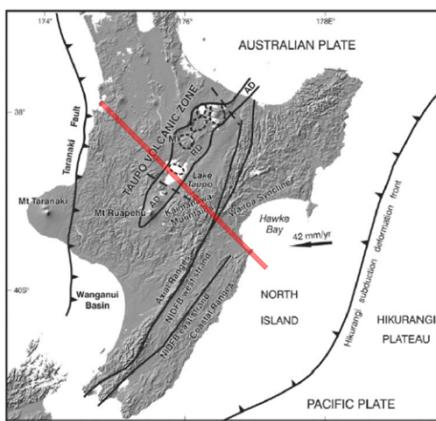
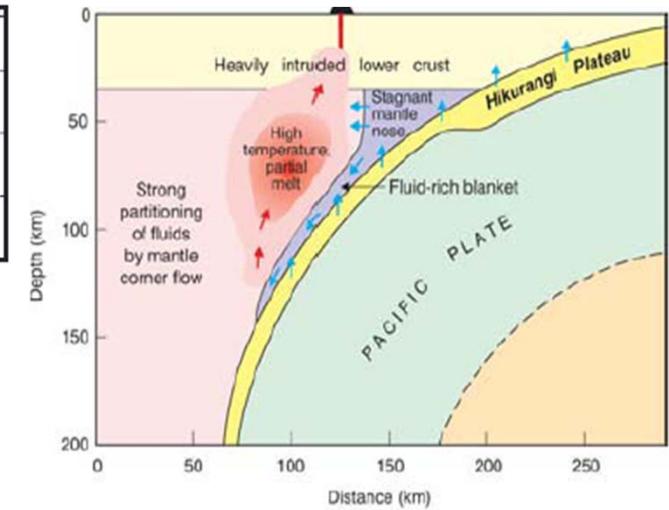
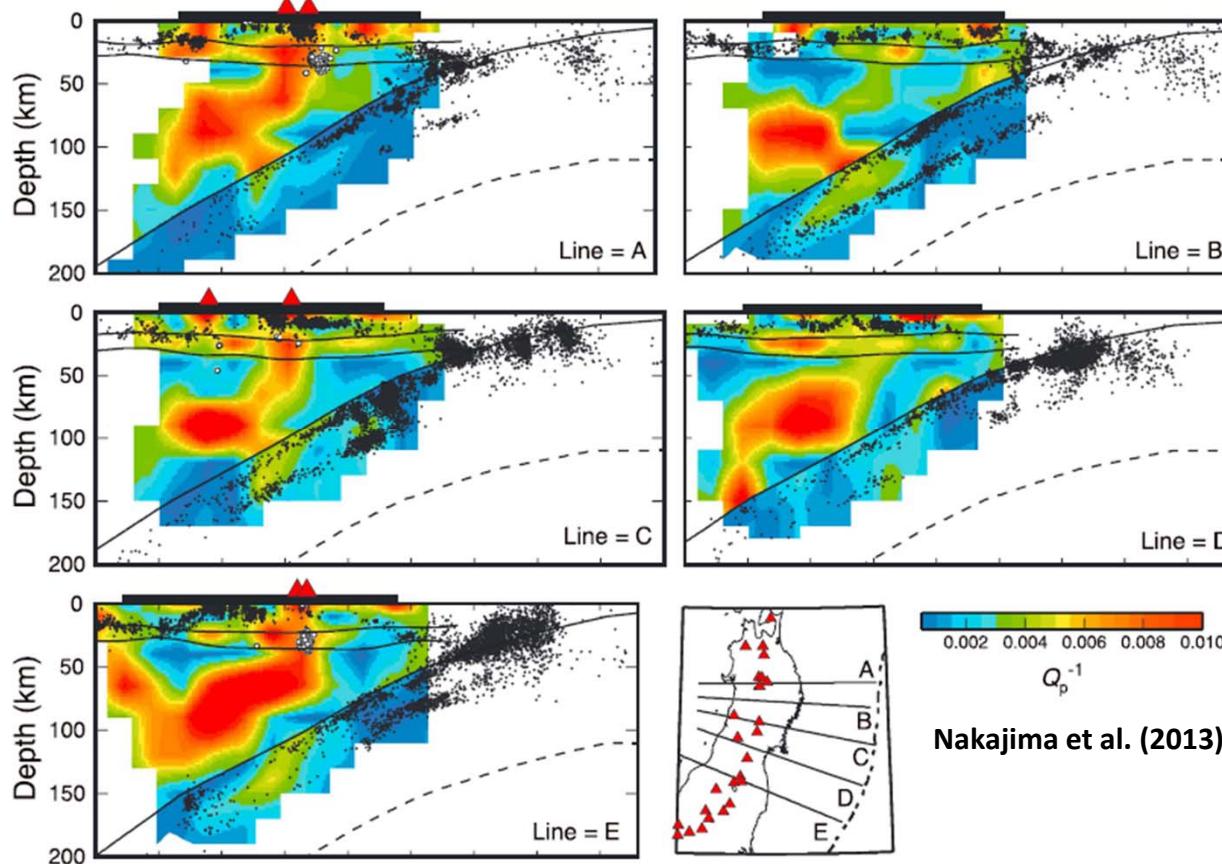
# seismic attenuation ( $Q^{-1}$ )

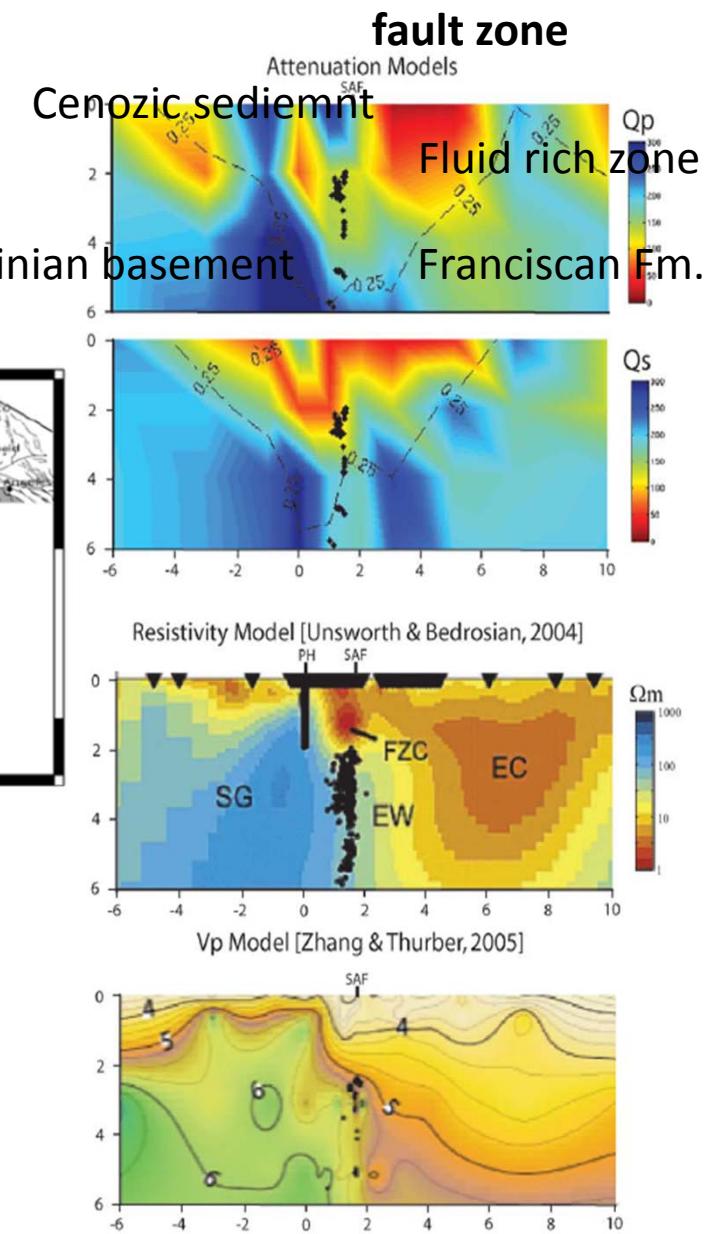
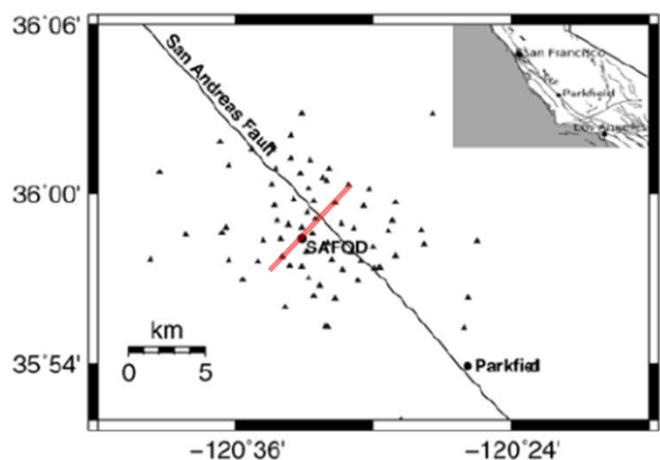


- Time domain: amplitude decay, longer duration
- Frequency domain: amplitude decay at high frequency
- Factors: temperature, fluid, cracks, permeability

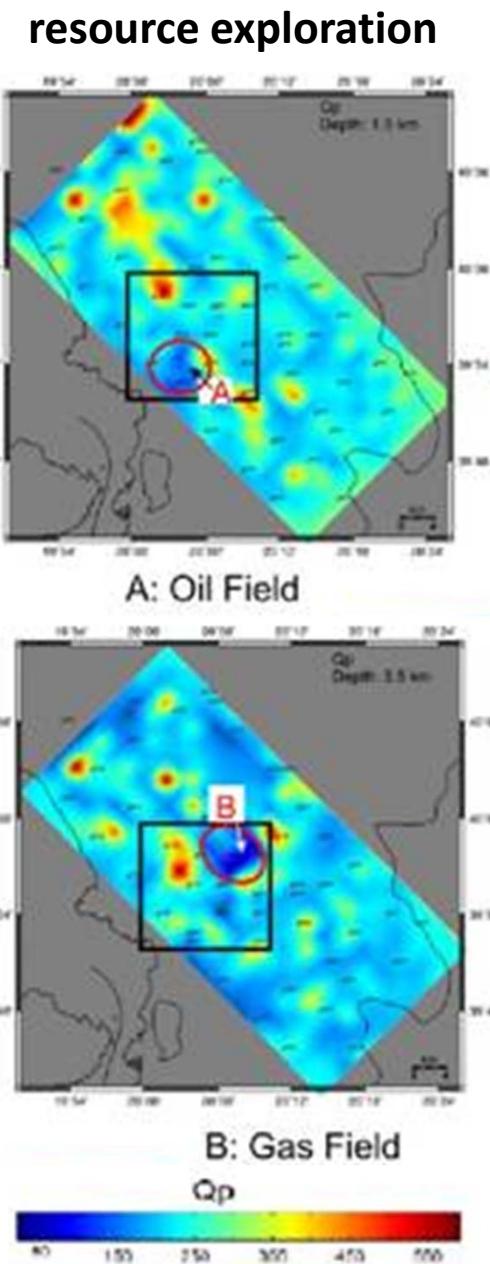


## Subduction zone/volcanoes



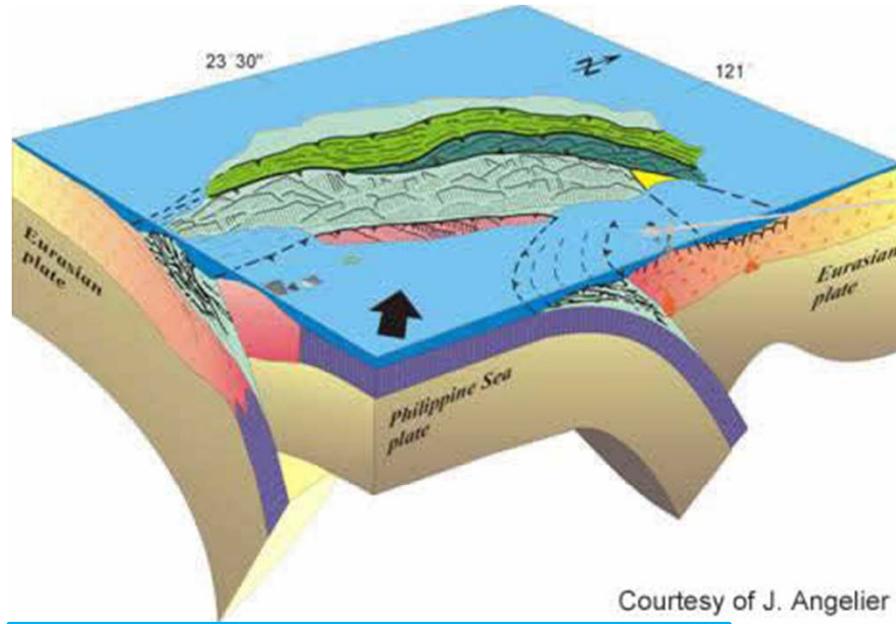


Bennington et al. (2008)

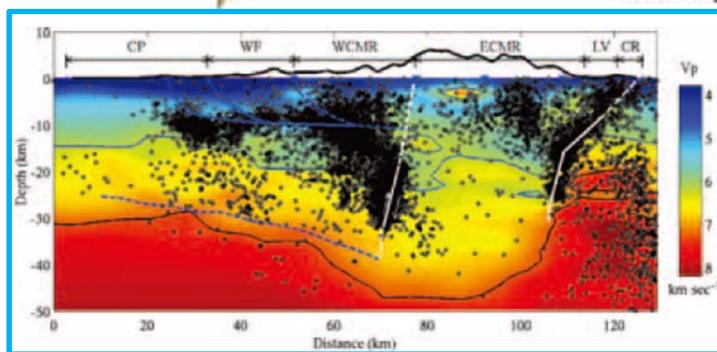


<http://www.landtechsa.com>

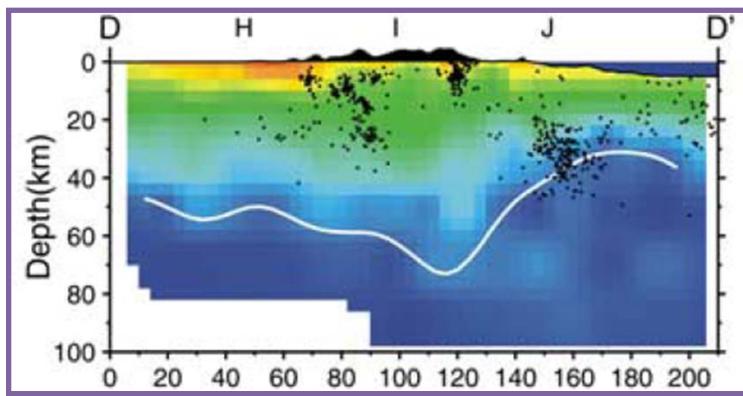
# The attenuation properties of the Taiwan orogenic structure



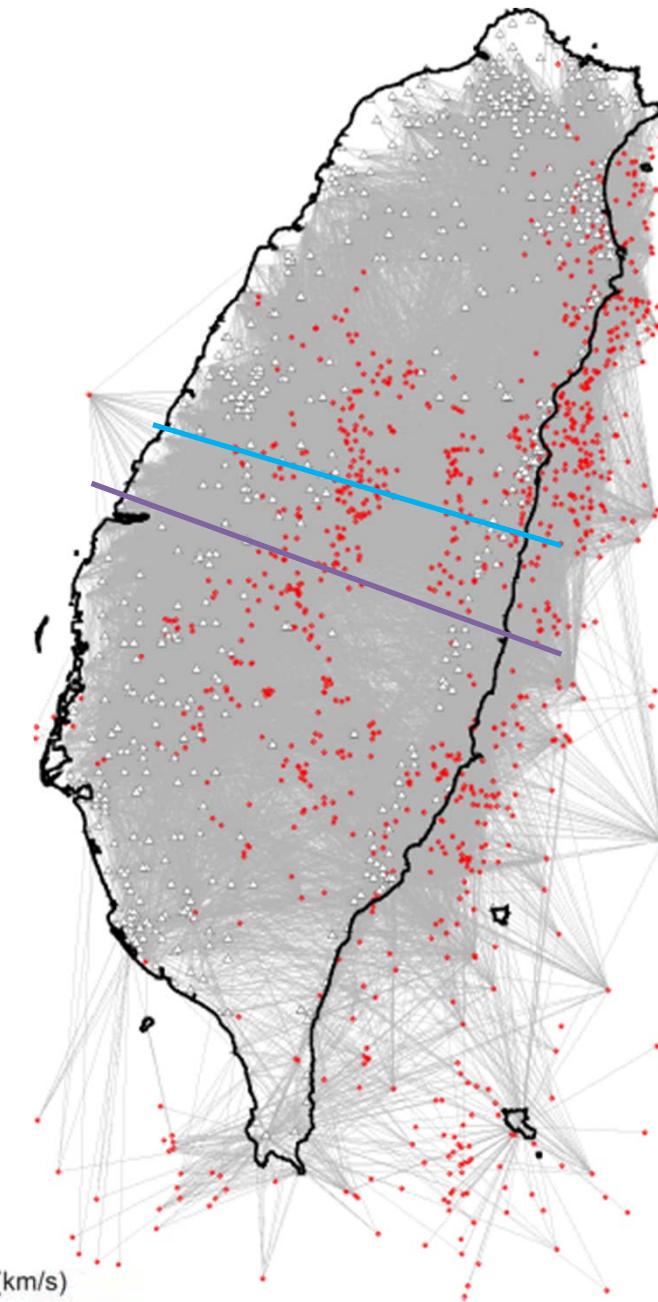
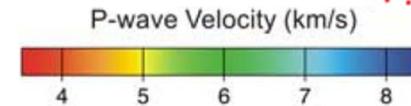
Courtesy of J. Angelier



Kim et al. (2005)



Wu et al. (2007)

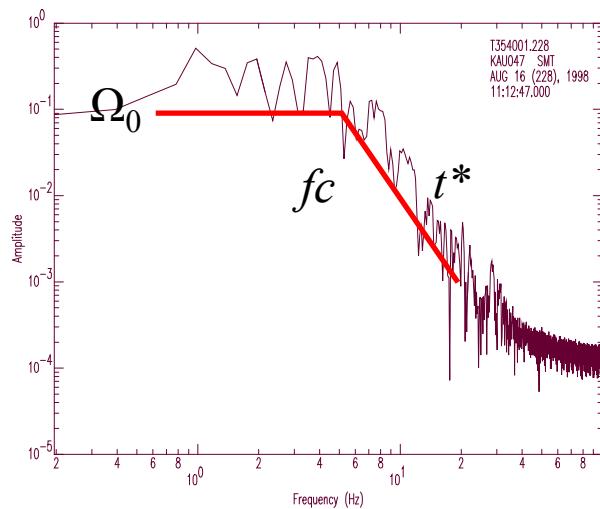
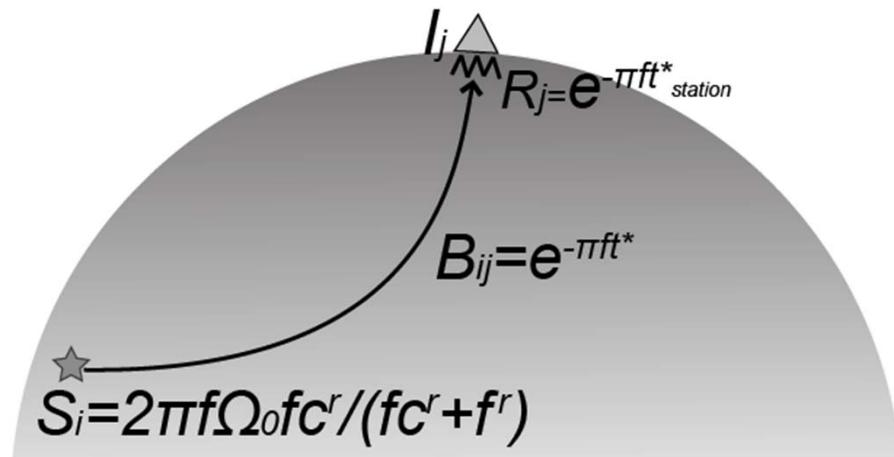


Wang et al. (2010)

# Q tomography

- *Observed velocity Spectrum:*

$$A_{ij}(f) = S_i(f) B_{ij}(f) R_j(f) I_j(f)$$



- *$\omega^2$ -source model assumption:*

$$A_{ij}(f) = 2\pi f \Omega_0 \frac{f_c^2}{f_c^2 + f^2} e^{-\pi f t^*}$$

(Eberhart-Phillips & Chadwick, 2002)

- *Q tomography:*

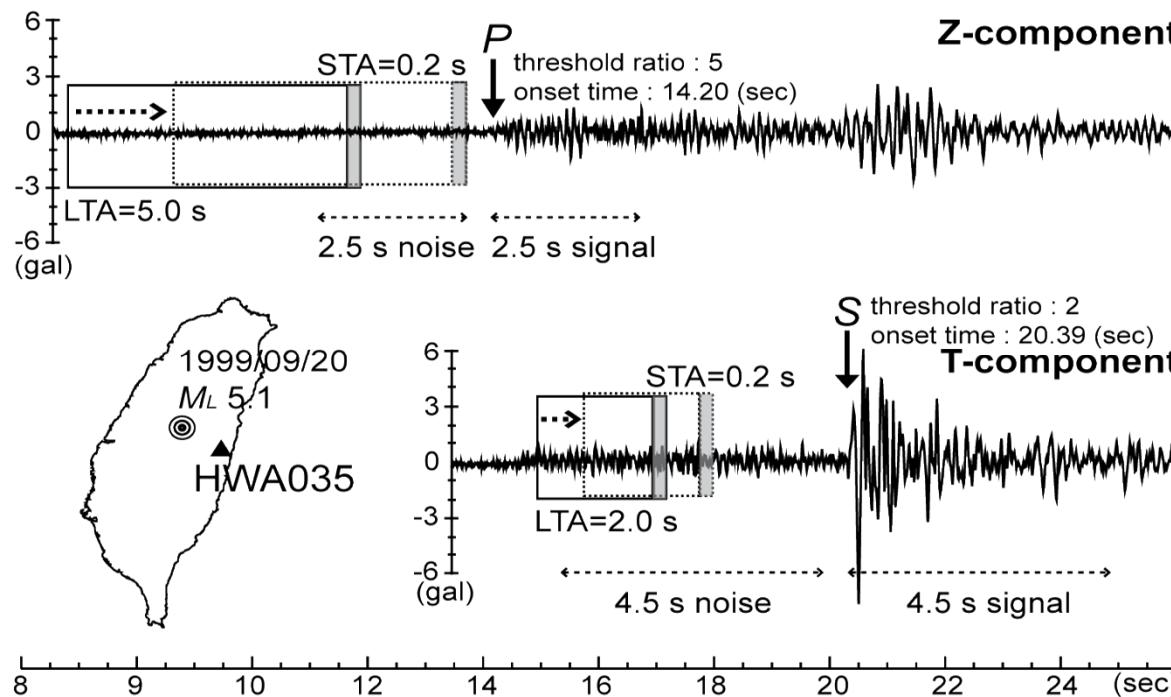
$$t^* = \int_{\text{source}}^{\text{receiver}} \frac{1}{Q(s)V(s)} ds$$

$f_c$  : corner frequency

$\Omega_0$  : spectrum plateau value

$t^*$  : whole-path attenuation operator

# Short-term average (STA) over long-term average (LTA) auto-picking algorithm

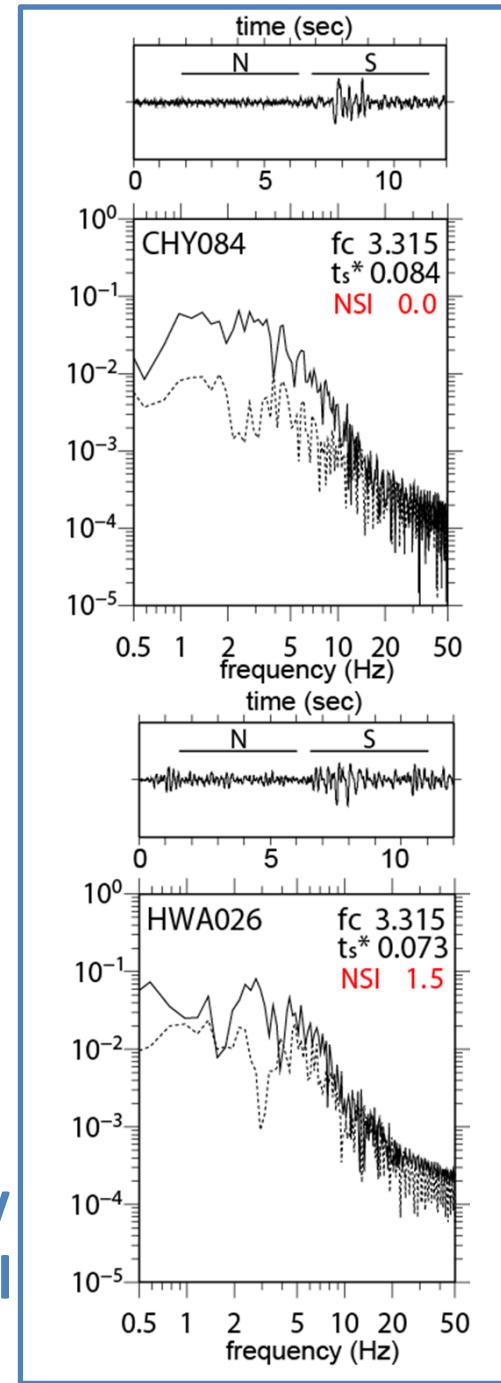



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D: duration in 2–30 Hz of signal-to-noise ratio > 4.5 for Qp (in 1–20 Hz of signal-to-noise ratio > 2.3 for Qs)

Quality		NSI
Best	$D \geq 80$ per cent	0.0
	$80 \text{ per cent} > D \geq 70 \text{ per cent}$	0.5
↓	$70 \text{ per cent} > D \geq 60 \text{ per cent}$	1.0
	$60 \text{ per cent} > D \geq 40 \text{ per cent}$	1.5
Bad	$40 \text{ per cent} > D$	2.0

FFT  
Data Quality Control



# two-steps of non-linear least-squares spectrum fitting

**observed spectrum**

↓ LSQENP →

$\Omega_0, \text{fc}, t^*$

↓ fix fc + LSQENP

$\Omega_0, t^*$

$\hat{Y}$ : predicted amplitude

$X$ : frequency points

$b_1 : \Omega_0$

$b_2 : \text{fc}$

$b_3 : t^*$

$$A_{ij}(f) = 2\pi f \Omega_0 \frac{f_c^2}{f_c^2 + f^2} e^{-\pi f t^*}$$

$$\hat{Y}_i = f_i(X_i; b_1, b_2, b_3)$$

$$\frac{\partial \sum_{i=1}^n [Y_i - \langle Y_i \rangle]^2}{\partial d_j} = 0$$

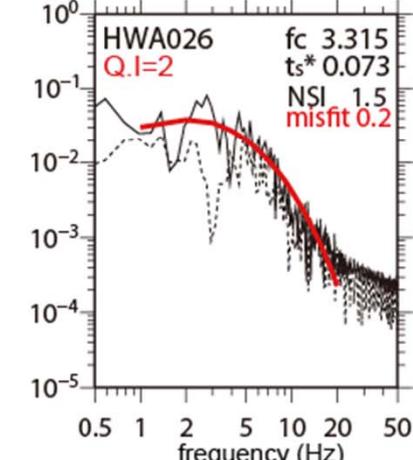
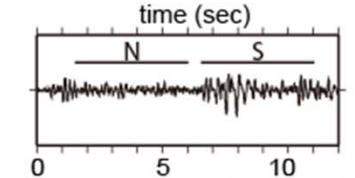
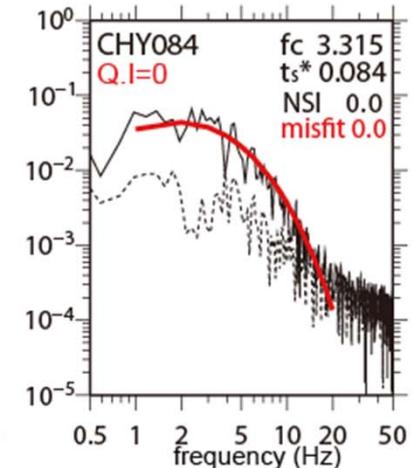
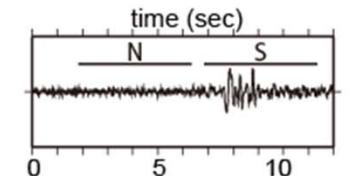
$$\begin{bmatrix} Y_1 - f_1 \\ Y_2 - f_2 \\ \vdots \\ Y_n - f_n \end{bmatrix} = \begin{bmatrix} \frac{\partial f_1}{\partial b_1} & \frac{\partial f_1}{\partial b_2} & \frac{\partial f_1}{\partial b_3} \\ \frac{\partial f_2}{\partial b_1} & \frac{\partial f_2}{\partial b_2} & \frac{\partial f_2}{\partial b_3} \\ \vdots & \vdots & \vdots \\ \frac{\partial f_n}{\partial b_1} & \frac{\partial f_n}{\partial b_2} & \frac{\partial f_n}{\partial b_3} \end{bmatrix} \begin{bmatrix} b_1 - \hat{b}_1 \\ b_2 - \hat{b}_2 \\ b_3 - \hat{b}_3 \end{bmatrix}$$

$$B = P \cdot \bar{d}$$

$$P^T P \bar{d} - P^T B = 0$$

$$\bar{d} = (P^T P)^{-1} P^T B$$

→ considering residual

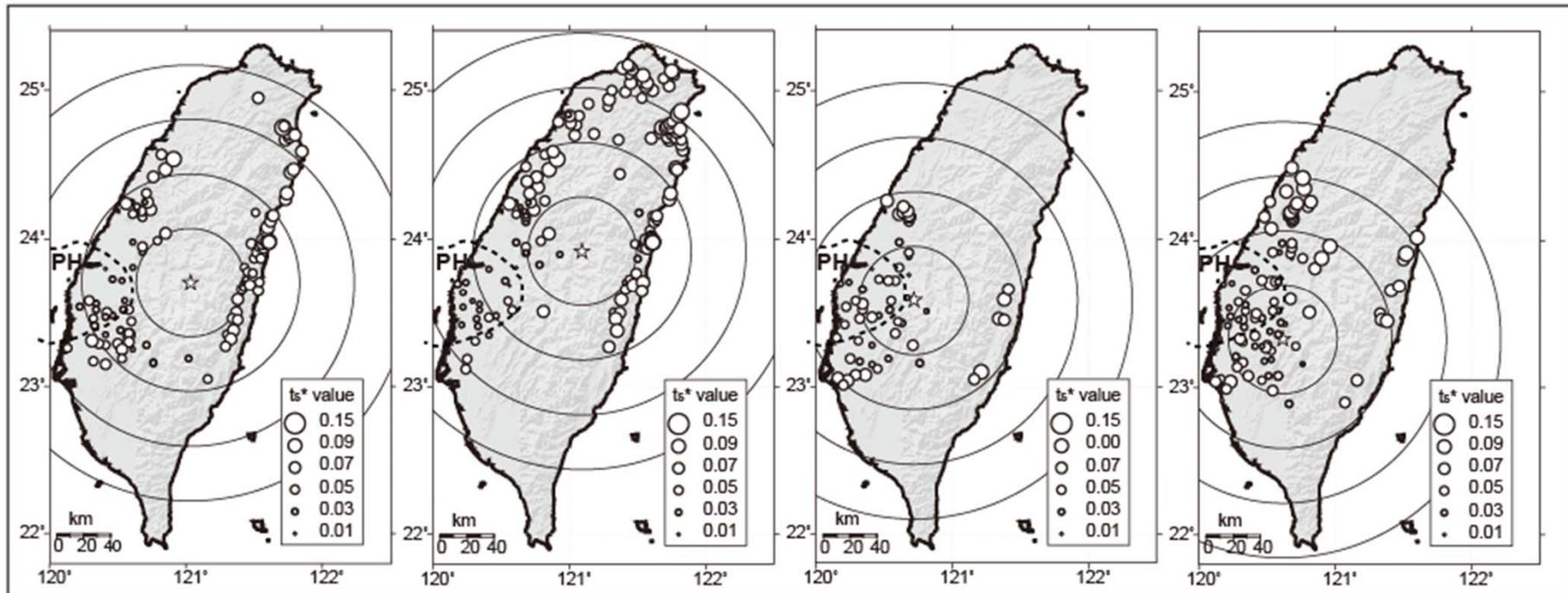
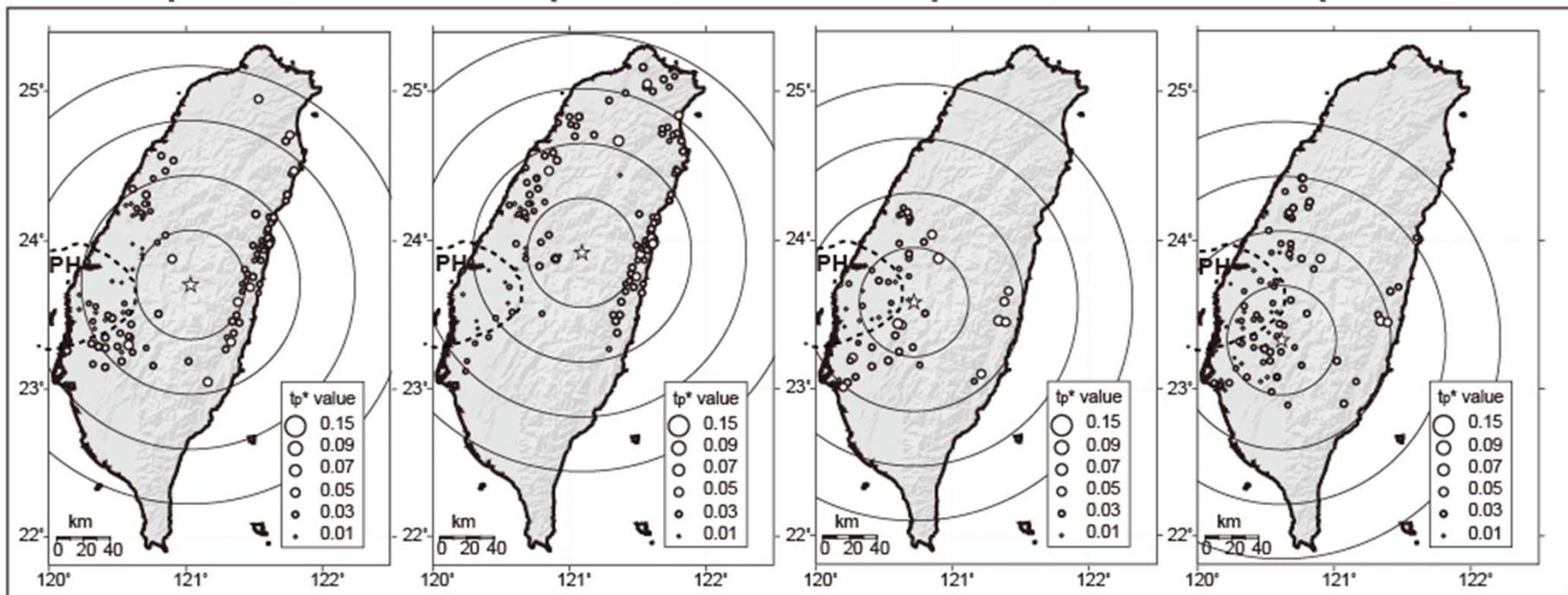


1999/10/18  $M_L$  5.2 Focal dep. 23.77 km

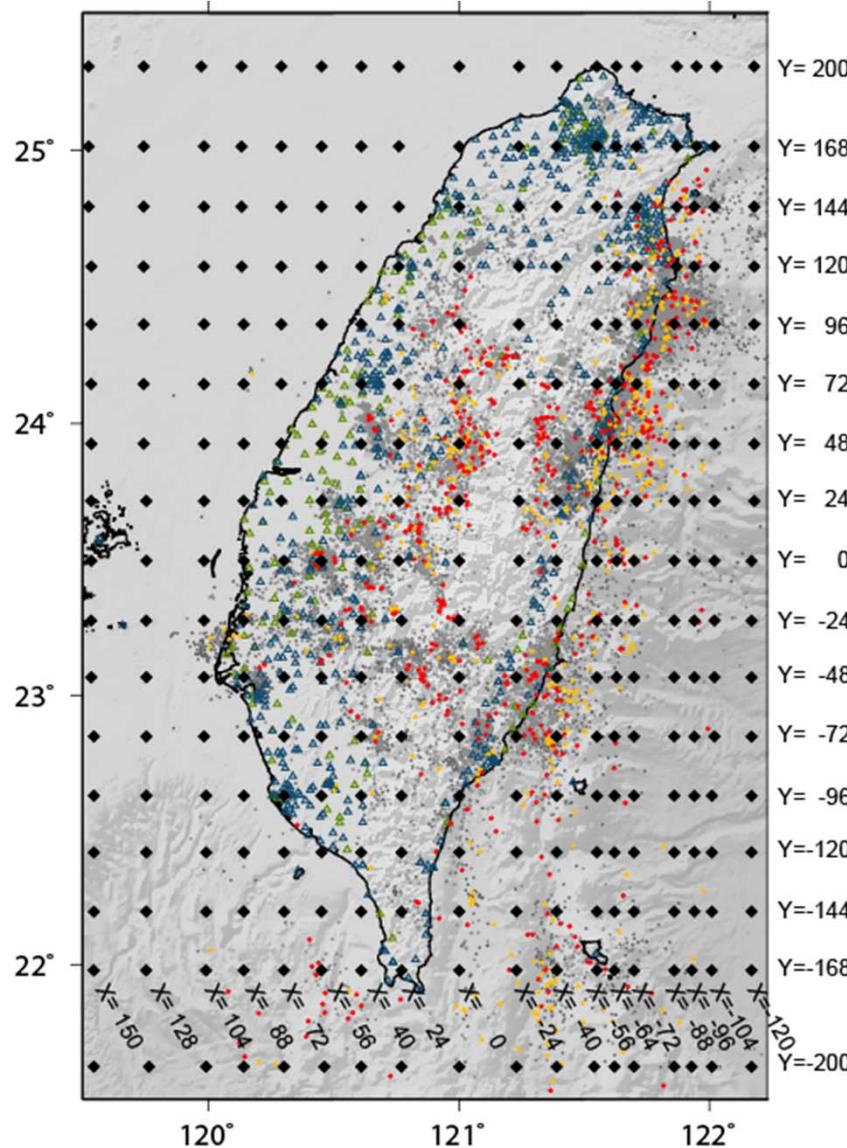
2000/06/19  $M_L$  5.2 Focal dep. 27.02 km

2001/02/18  $M_L$  4.9 Focal dep. 17.67 km

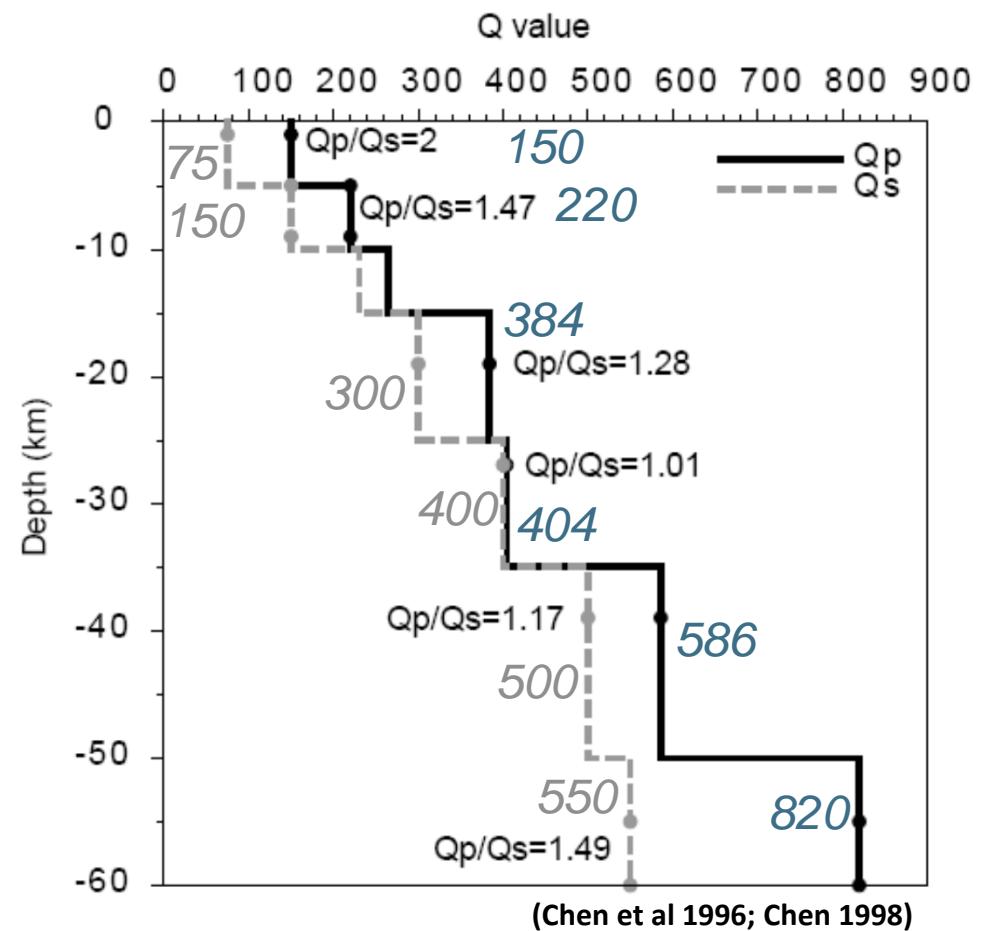
2002/09/30  $M_L$  5.0 Focal dep. 8.12 km



# Model grid



# Initial Qp, Qs model



- *Vp & Vs models*

(Kim et al. 2005)

# Spread function

$$M^{est} = RM^{true}$$

$$\begin{bmatrix} m_1 \\ m_2 \\ \vdots \\ m_j \end{bmatrix} = \begin{bmatrix} r_{11} & \cdots & r_{1k} \\ \vdots & \ddots & \vdots \\ r_{j1} & \cdots & r_{jk} \end{bmatrix} \begin{bmatrix} m_1' \\ m_2' \\ \vdots \\ m_j' \end{bmatrix}$$

resolution matrix

$$\text{if } M^{est} = M^{true}$$

$$\begin{aligned} \text{then } r_{jk} &= 0, j=k \\ r_{jk} &\neq 0, j \neq k \end{aligned}$$

$$R = \begin{bmatrix} 1 & 0 & \dots & 0 \\ 0 & 1 & 0 & \vdots \\ \vdots & 0 & \ddots & 0 \\ 0 & \dots & 0 & 1 \end{bmatrix}$$

$$S_j = \log \left[ \left| s_j \right|^{-1} \sum_{k=1}^N \left( \frac{s_{kj}}{\left| s_j \right|} \right)^2 \right] D_{jk}$$

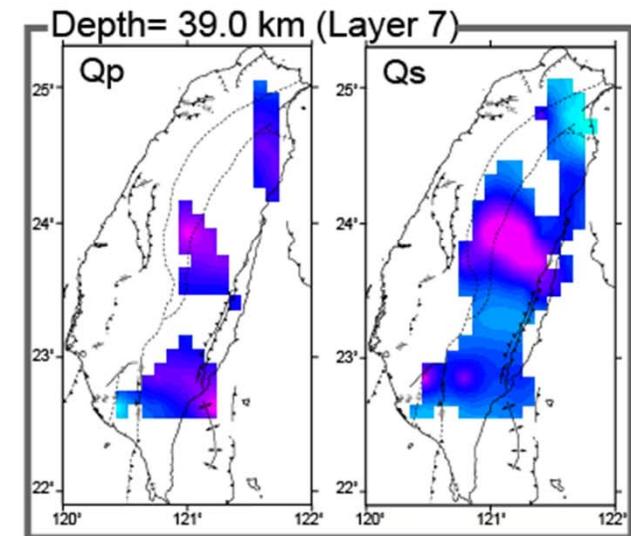
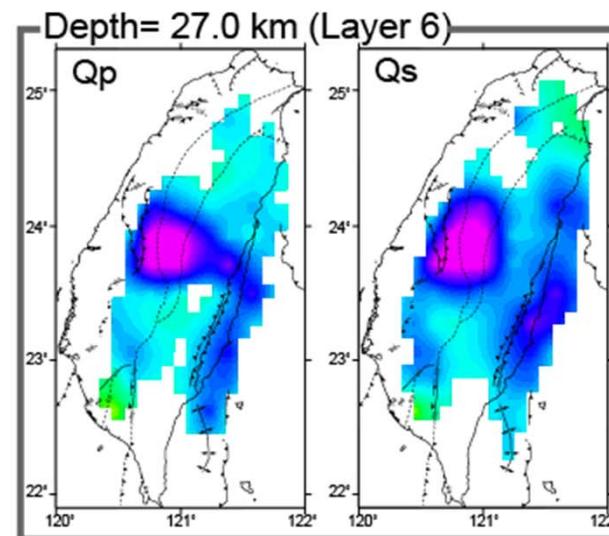
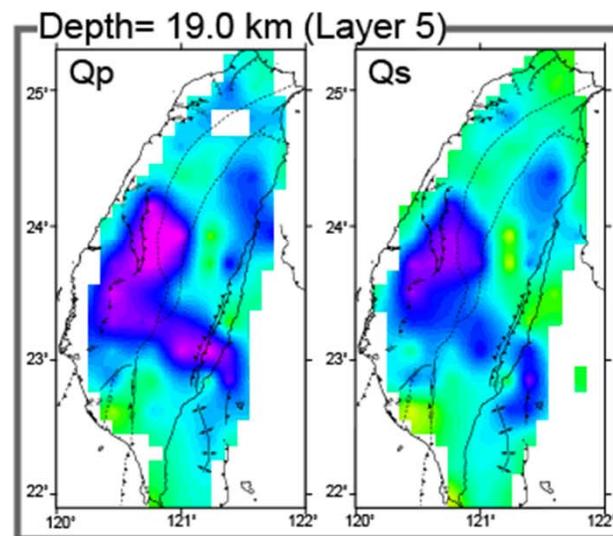
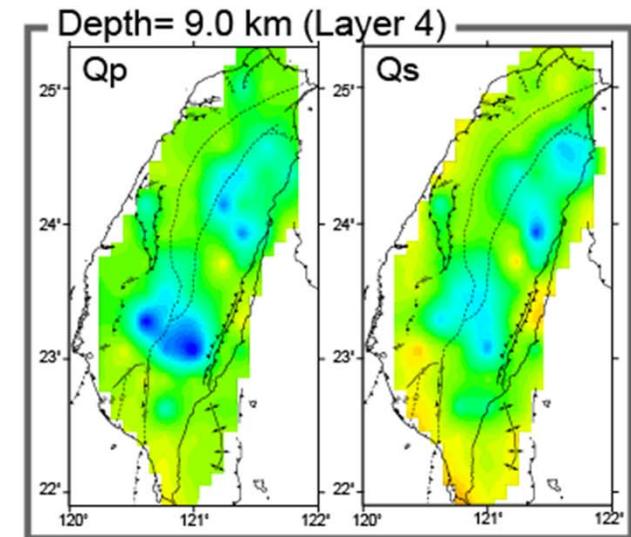
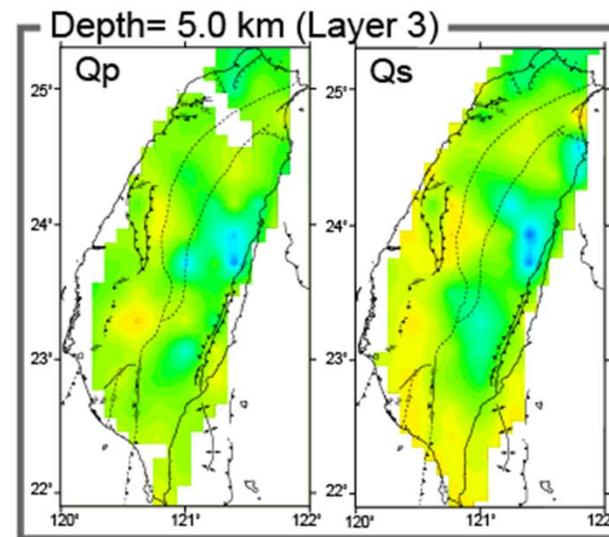
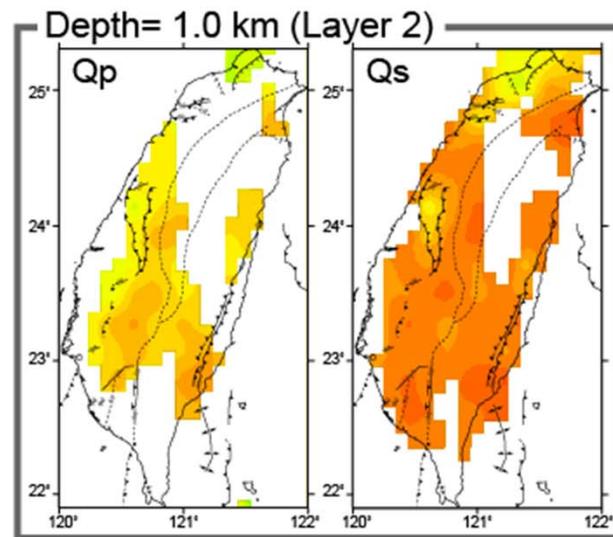
Michelinin and McEvilly (1991)

$$j \underbrace{\begin{bmatrix} S_1 & S_{21} & \cdot & \cdot & S_{k1} \\ 0 & S_2 & 0 & 0 & 0 \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ \cdot & \cdot & \cdot & \cdot & \cdot \\ S_{1j} & 0 & 0 & 0 & S_j \end{bmatrix}}_k$$

$D_{jk}$

- *larger  $S_j$ , more smearing*

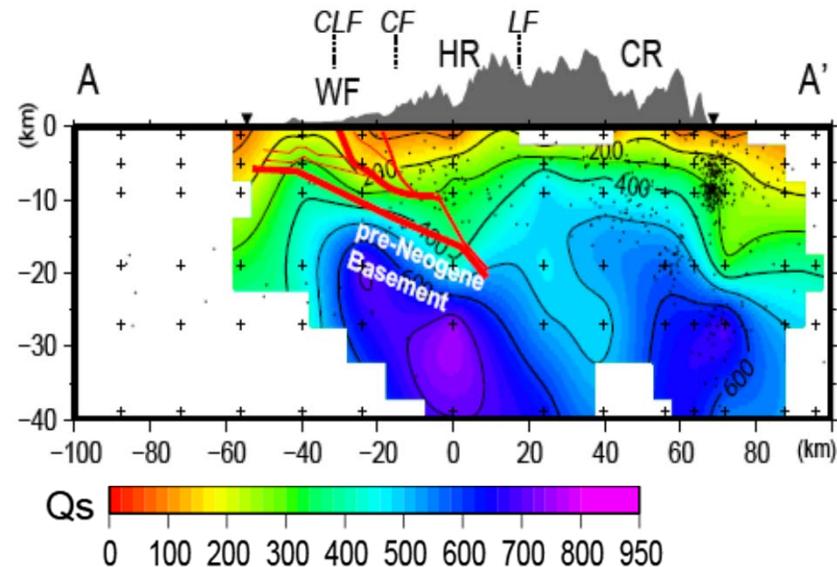
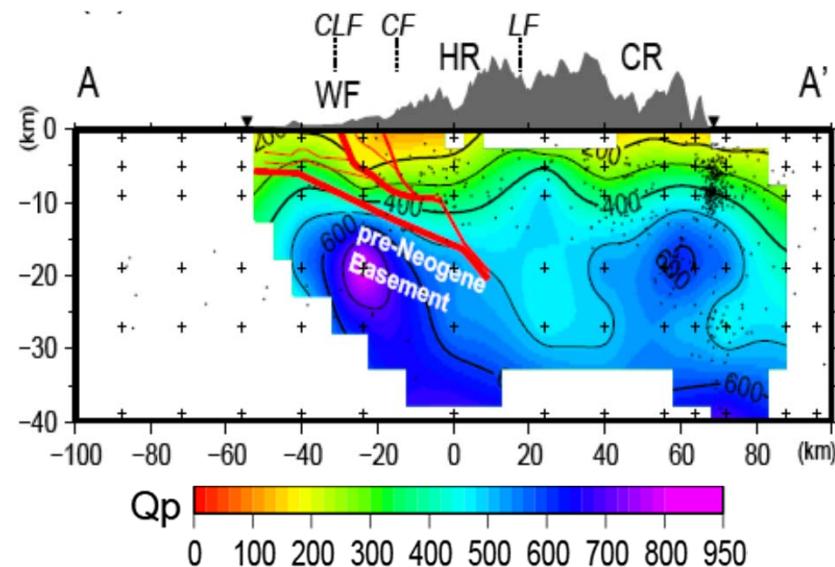
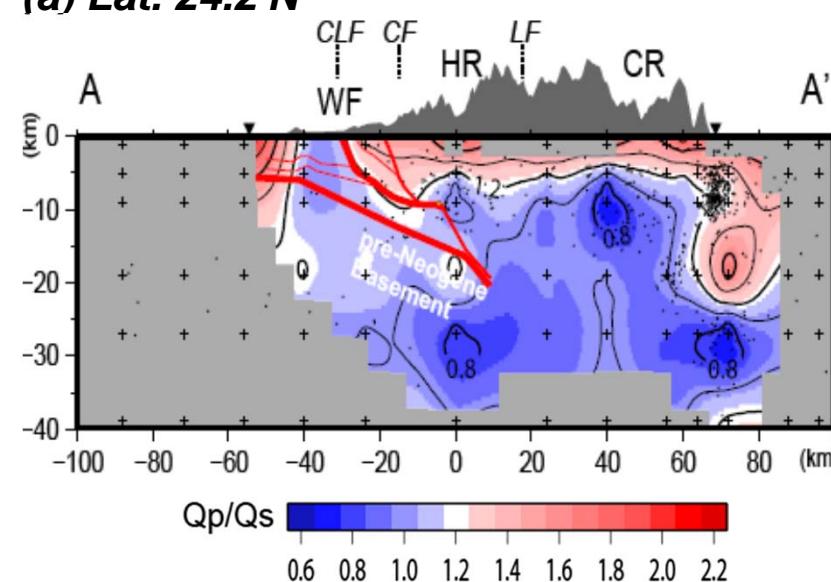
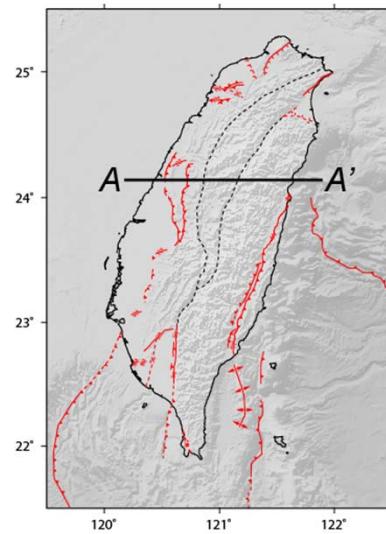
# Q<sub>p</sub>, Q<sub>s</sub> Tomography images



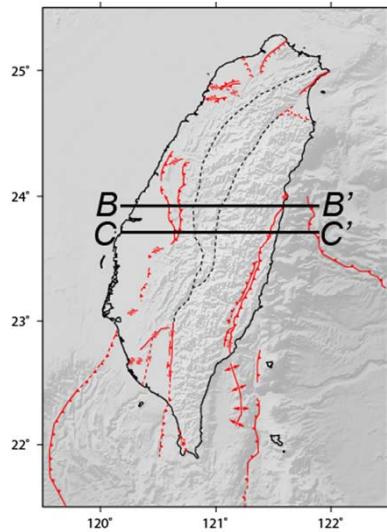
Wang et al. (2010)

# Chelungpu Fault

(a) Lat. 24.2°N



Wang et al. (2010)



# Peikang High \ Central Range

## Peikang High

✓ High Qp, Qs

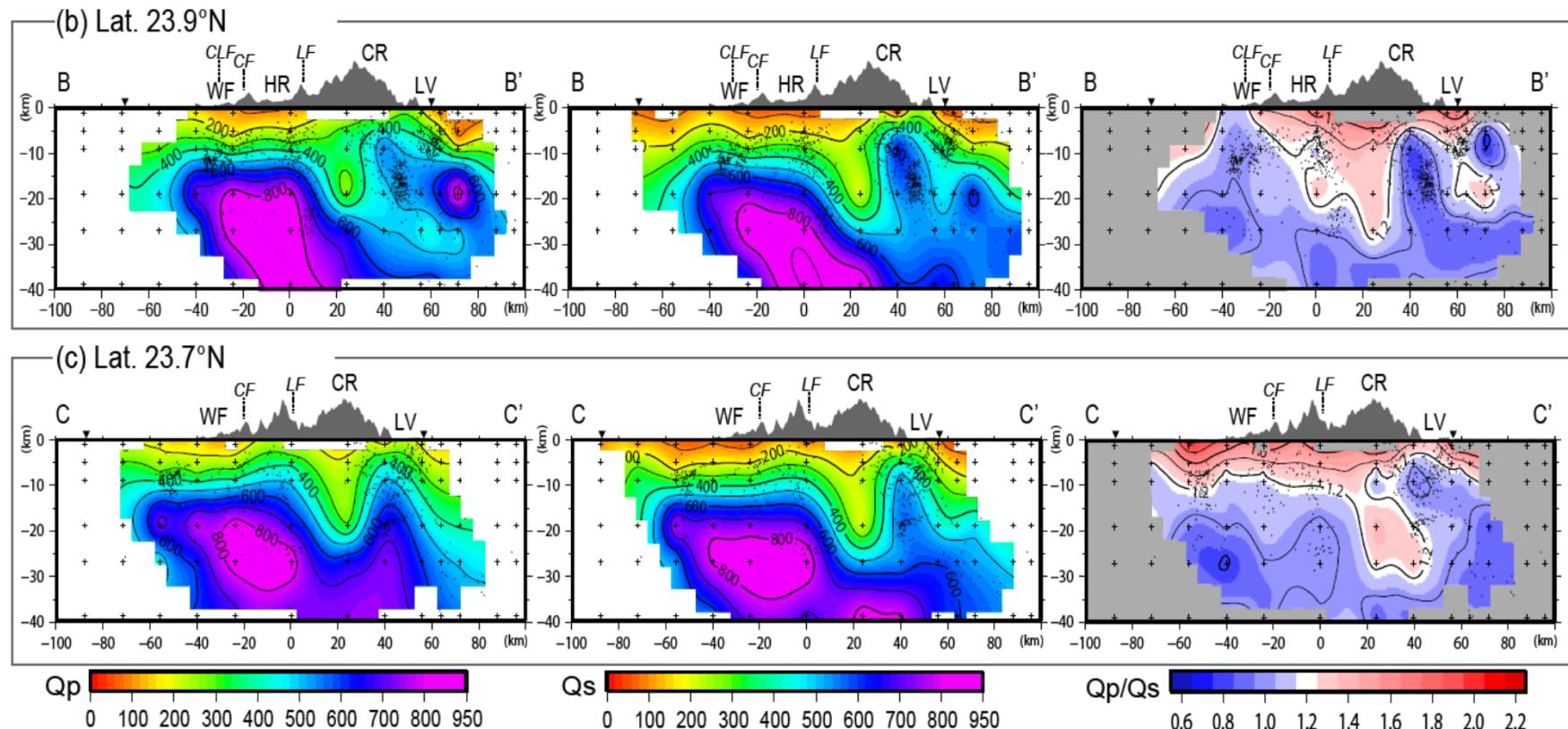
## Central Range

✓ Aseismic Zone

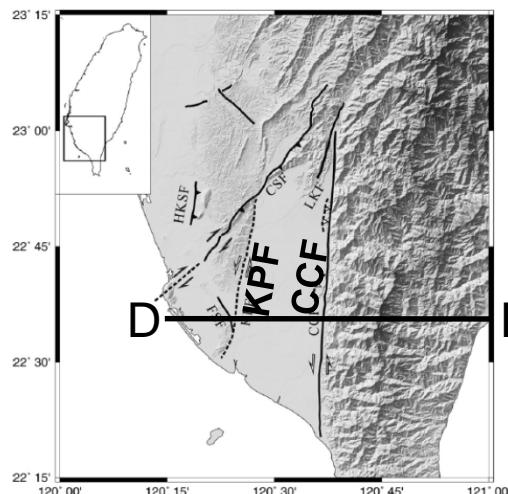
✓ High Temperature

(*Ma et al. 1996; Lin 2000;  
Simoes et al. 2007; Yamato et al. 2008*)

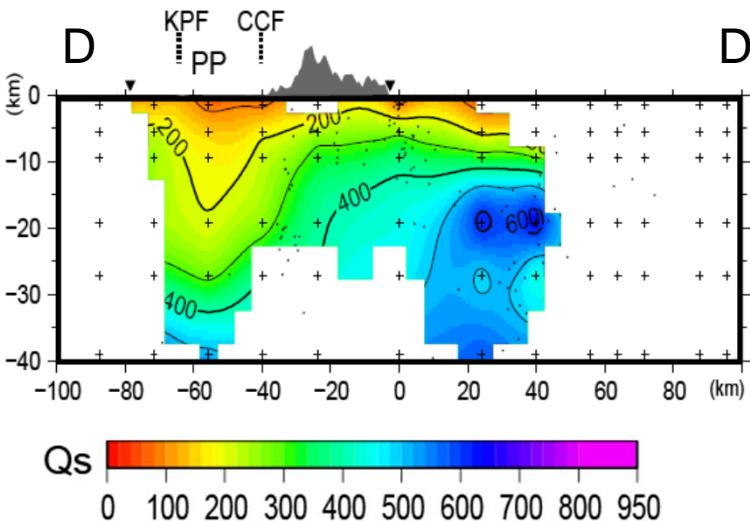
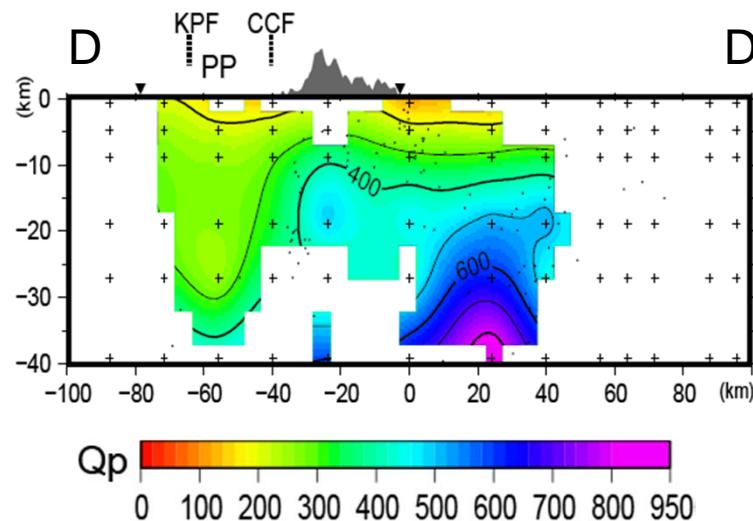
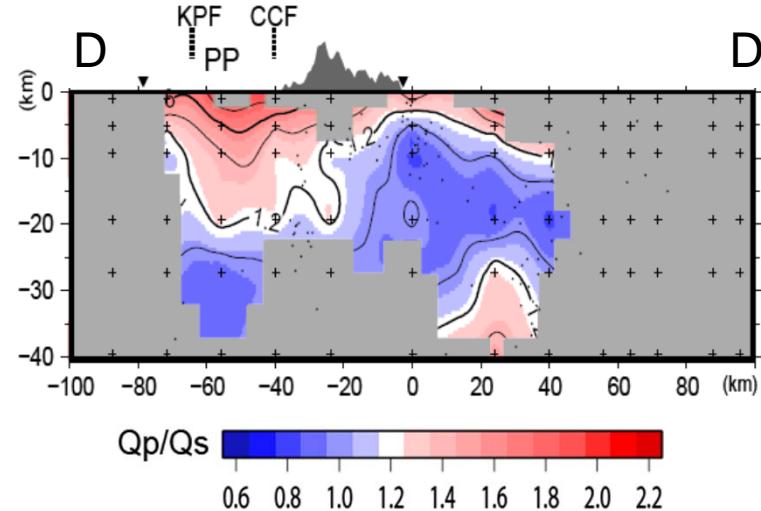
✓ Ductile (*Kim et al. 2005*)



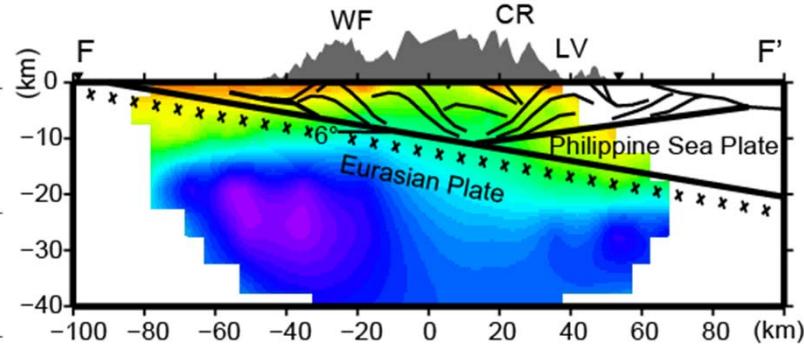
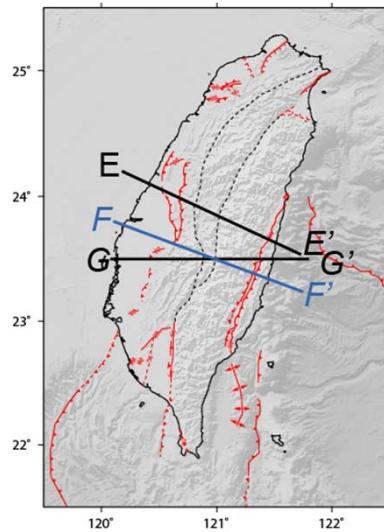
# Pingtung Plain



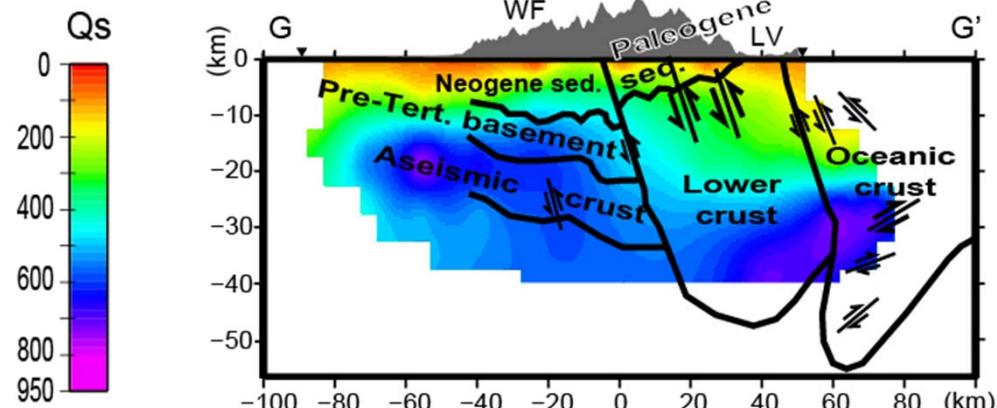
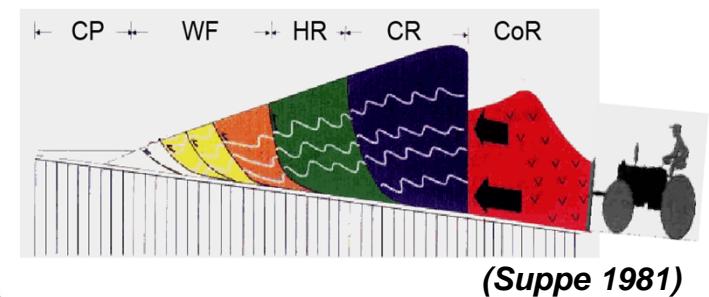
(d) Lat. 22.6°N



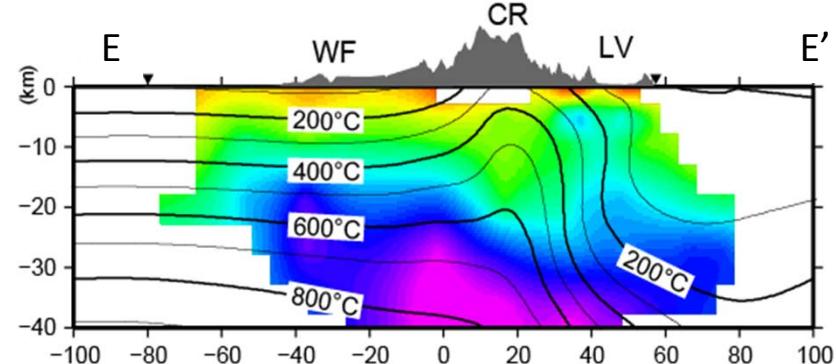
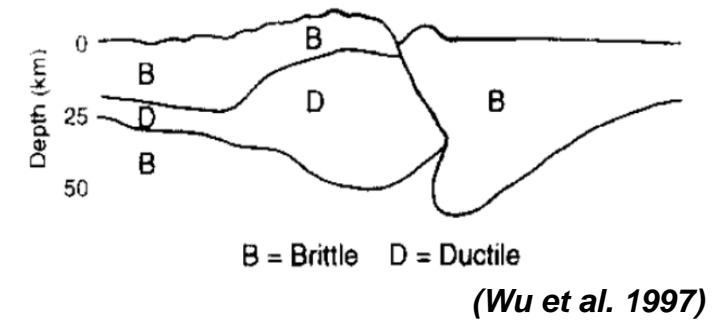
- High Qp/Qs, low Qp, Qs are associated with the **unconsolidated coastal and estuarine sediments** within **fully fluid-saturated** property of Pingtung Plain.



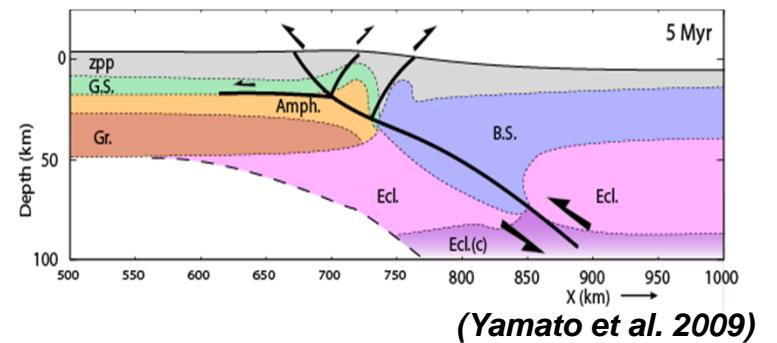
### ● Thin-skinned model

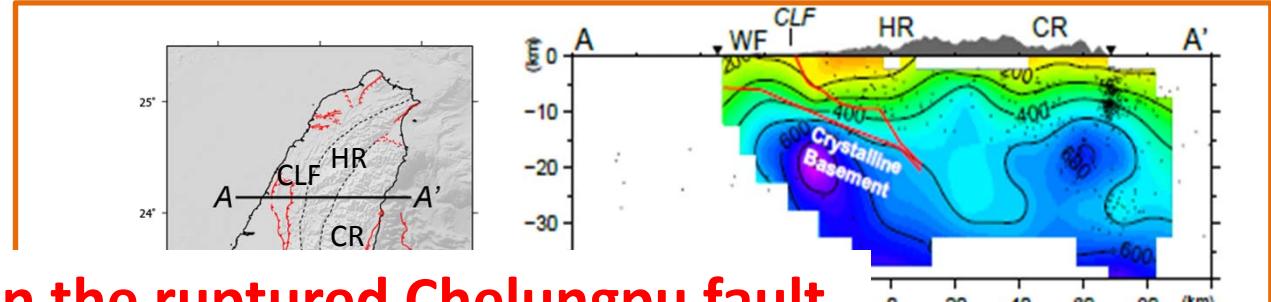


### ● Lithospheric collision model



### ● Thermo-mechanical model



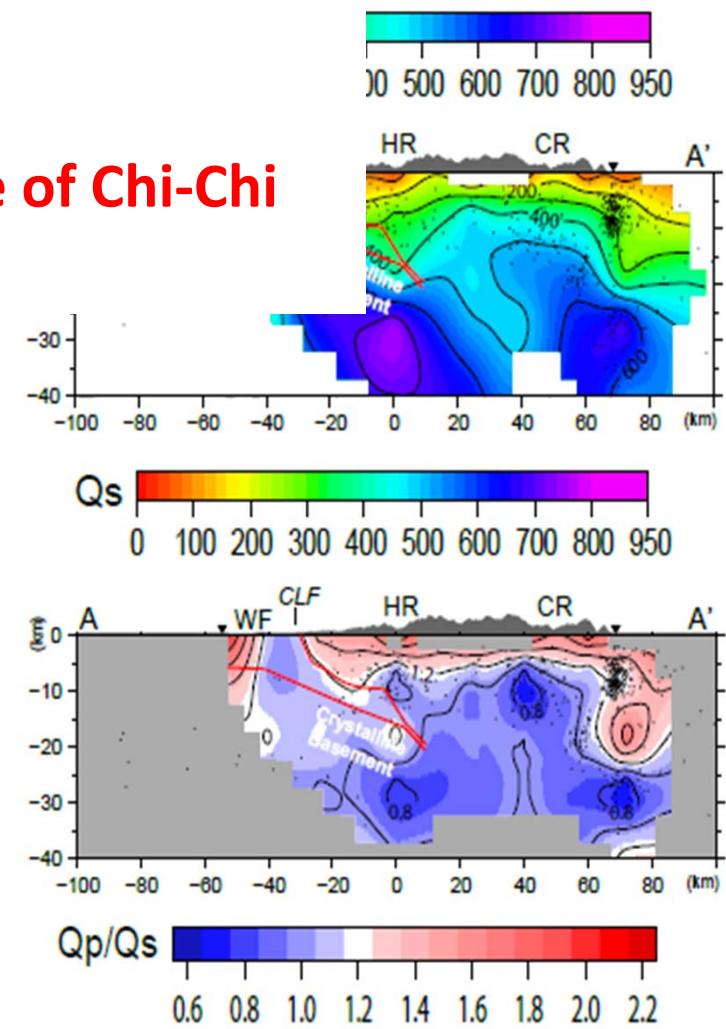


## How is the Q within the ruptured Chelungpu fault zone?

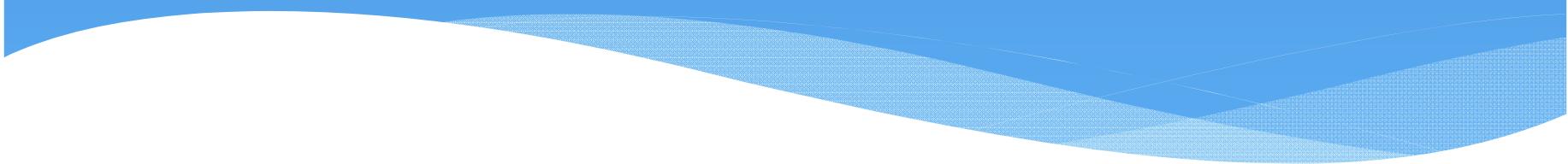
$Q_f$  Is the low Q related to the occurrence of Chi-Chi earthquake? Yes!

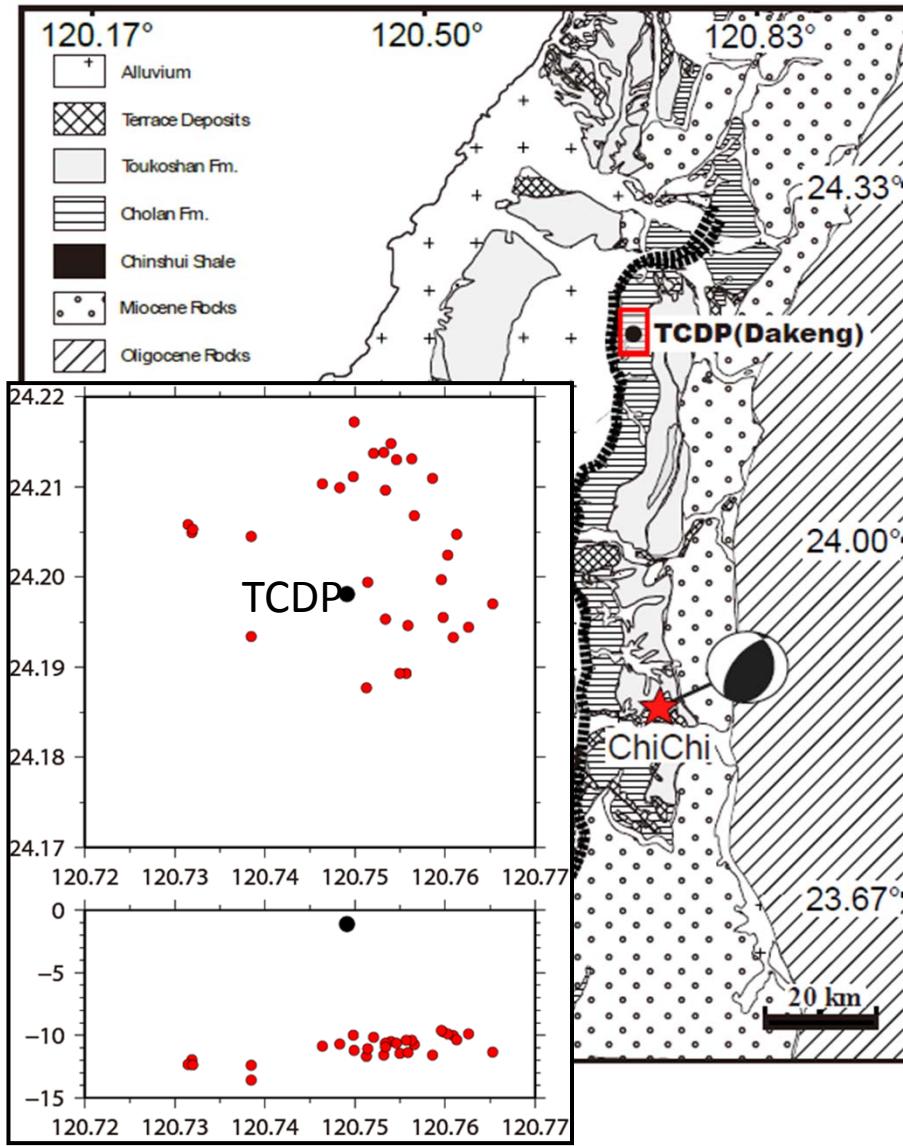
(Sanders et al., 1995)

Rock State Change	Seismic Parameter Change			
	$Q_s$	$Q_p$	$Q_p/Q_s$	$V_p/V_s$
Increase temperature	smaller	smaller	larger	larger
Partial melt	much	smaller	much	much
	smaller		larger	larger
Increase fracture abundance (Increase fluid)	smaller	smaller	larger	larger
Add gas or supercritical	larger	much	much	smaller
		smaller	smaller	



# The attenuation features within the Chelungpu fault zone



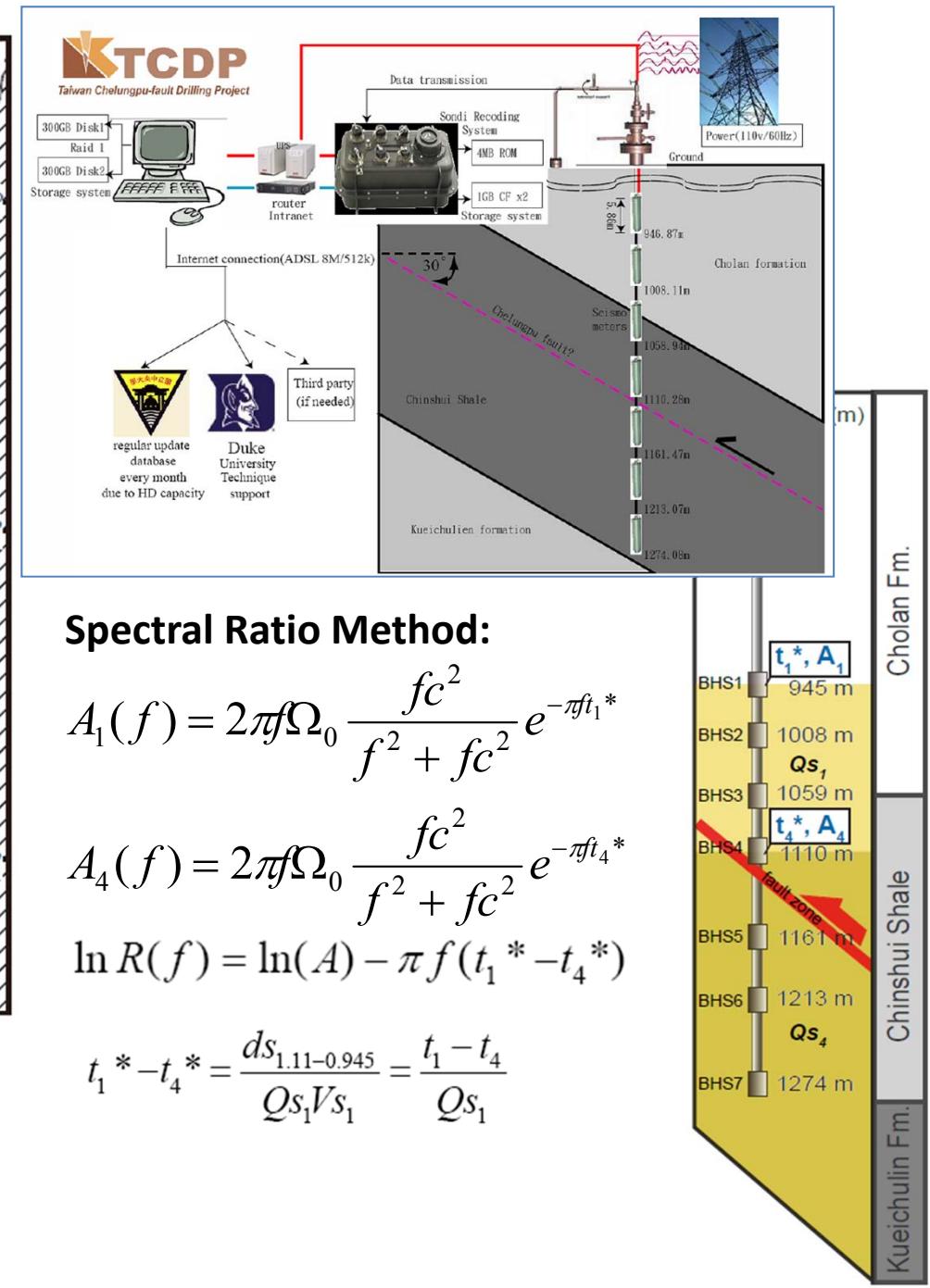


2006/11-2007/4

Incident angle < 10°

Total 26 events with high S/N were used.

Mw 0.28-1.5



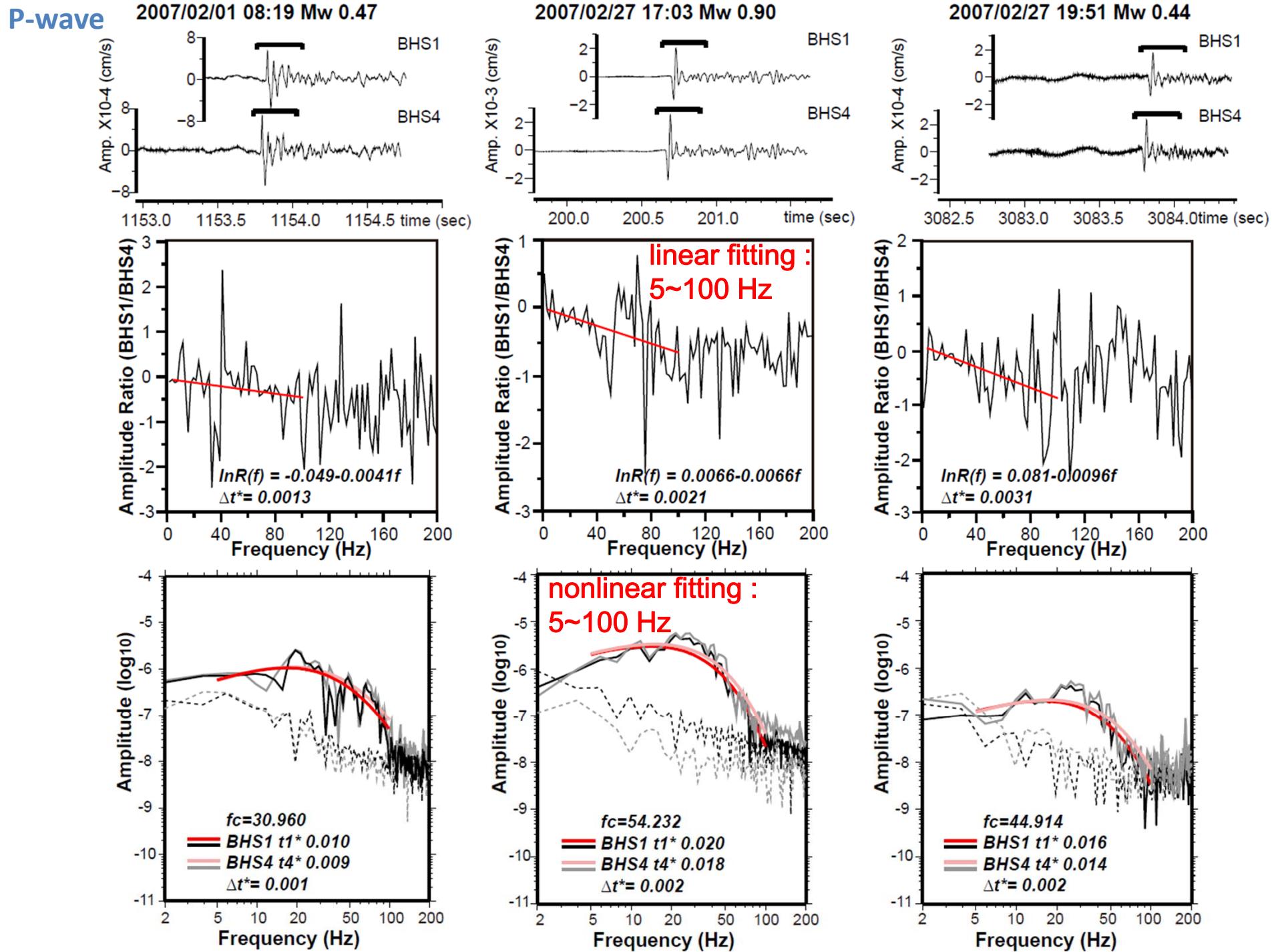
### Spectral Ratio Method:

$$A_1(f) = 2\pi f \Omega_0 \frac{fc^2}{f^2 + fc^2} e^{-\pi f t_1^*}$$

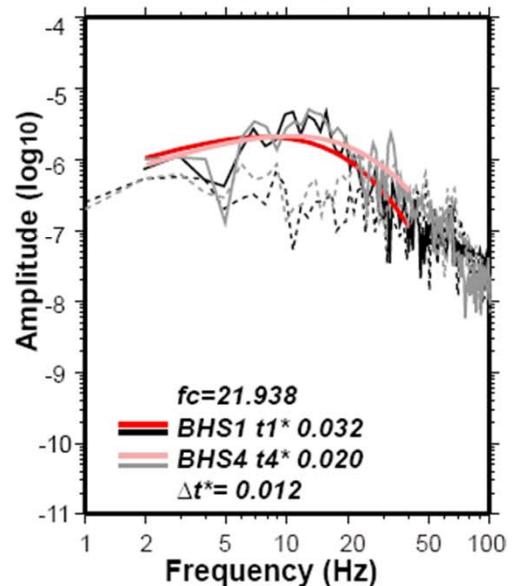
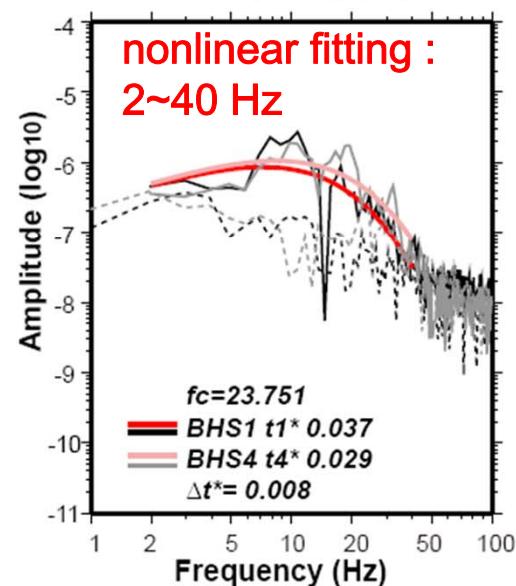
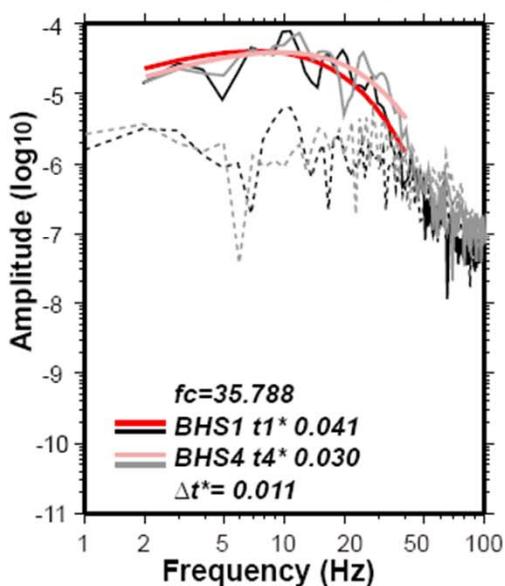
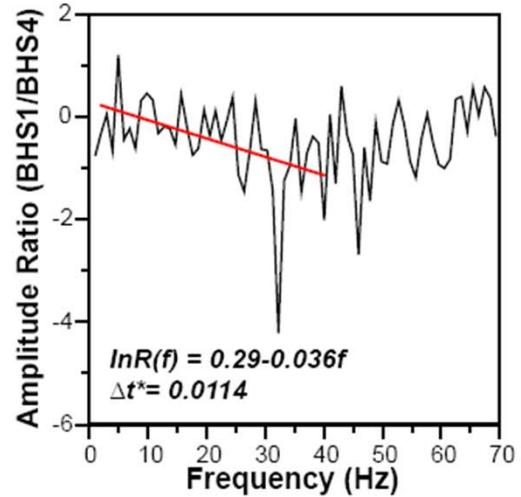
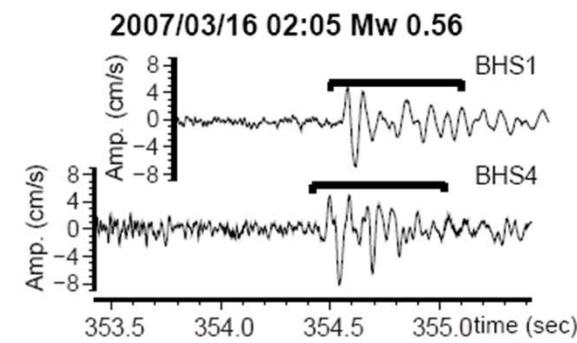
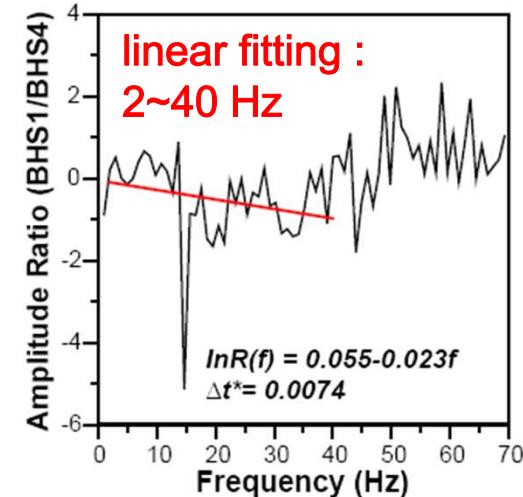
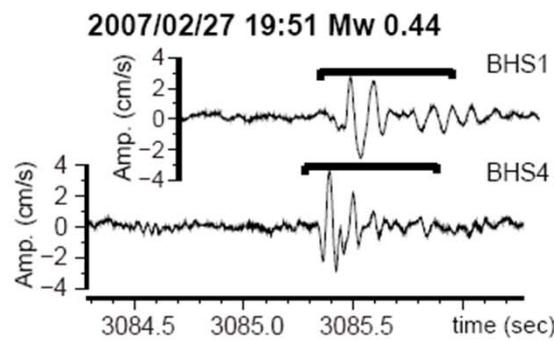
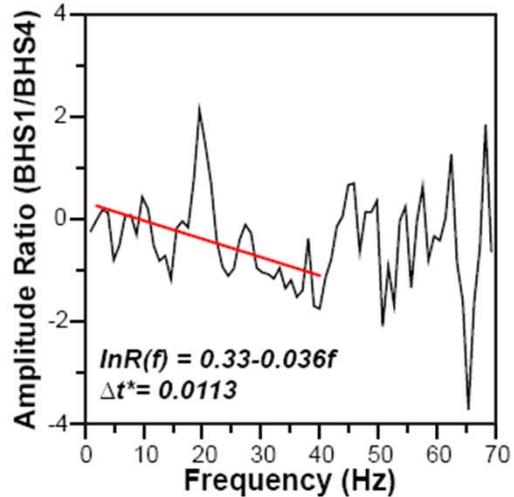
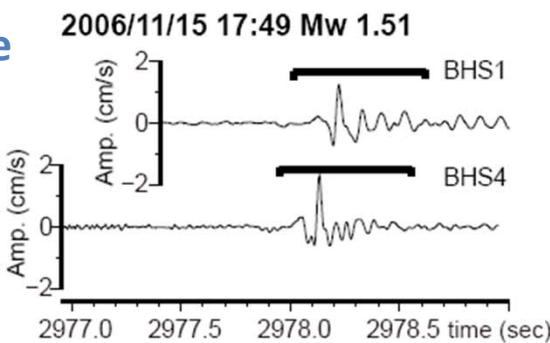
$$A_4(f) = 2\pi f \Omega_0 \frac{fc^2}{f^2 + fc^2} e^{-\pi f t_4^*}$$

$$\ln R(f) = \ln(A) - \pi f(t_1^* - t_4^*)$$

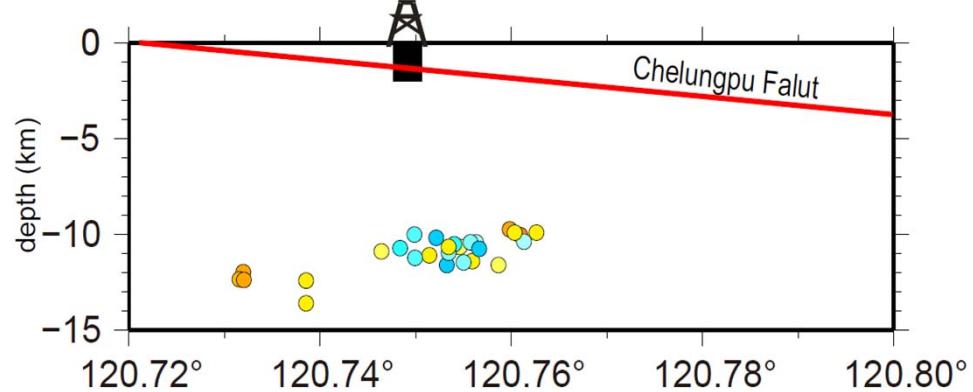
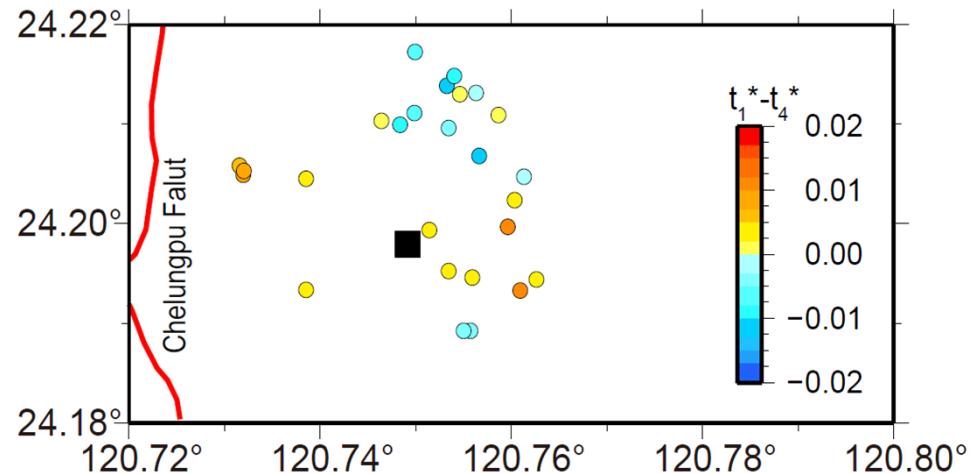
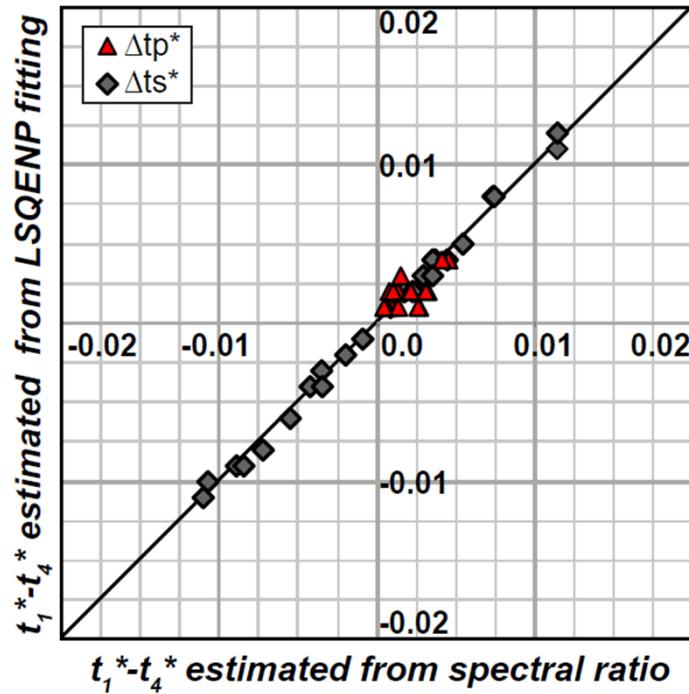
$$t_1^* - t_4^* = \frac{ds_{1.11-0.945}}{Qs_1 V s_1} = \frac{t_1 - t_4}{Qs_1}$$



## S-wave

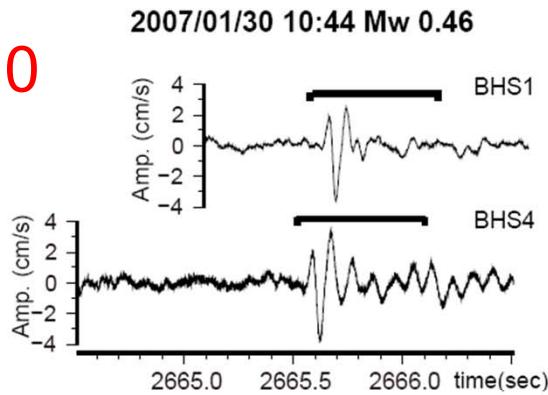


# The estimation of $t^*$

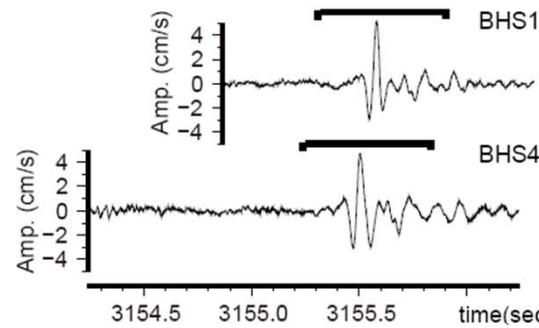


$$t_1^* - t_4^* < 0$$

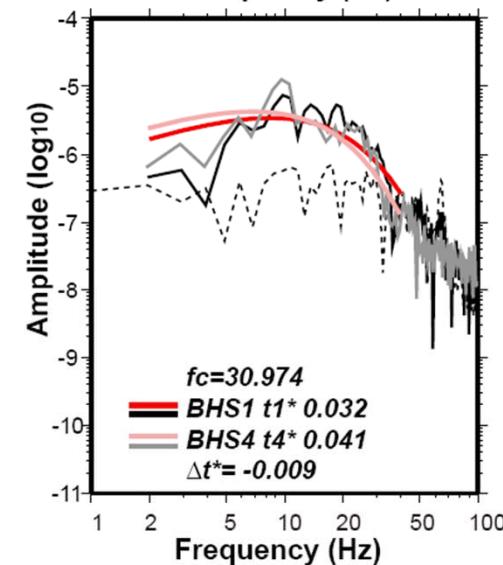
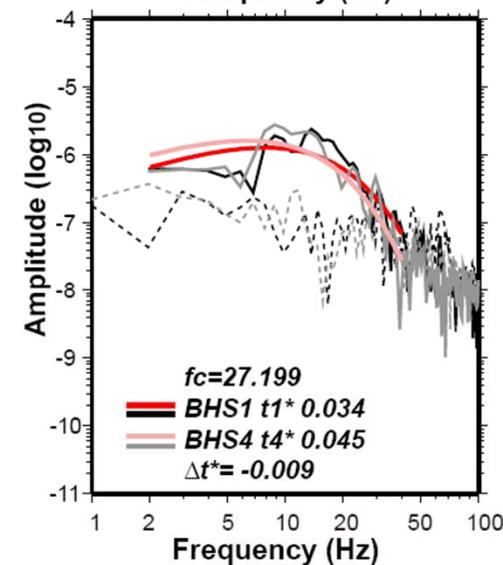
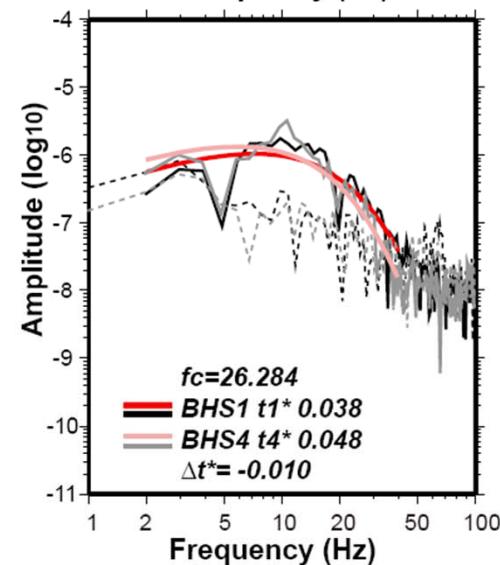
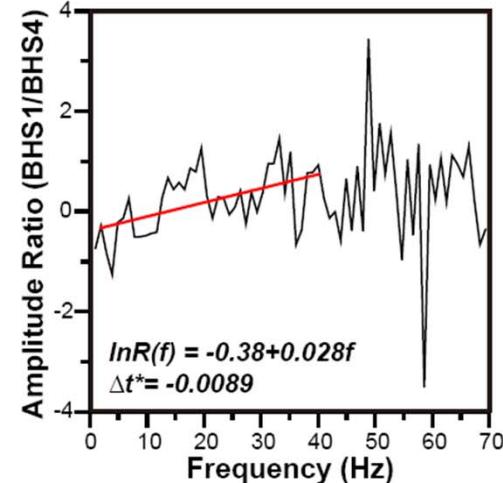
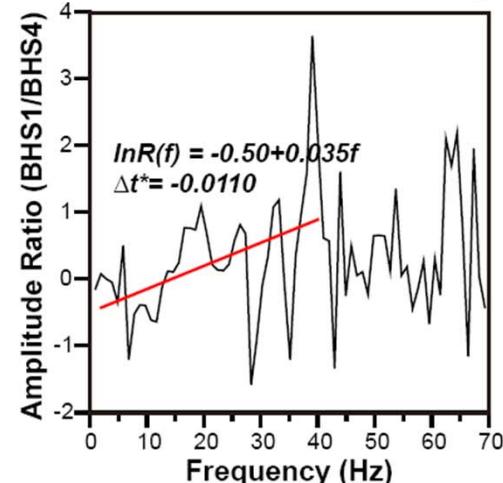
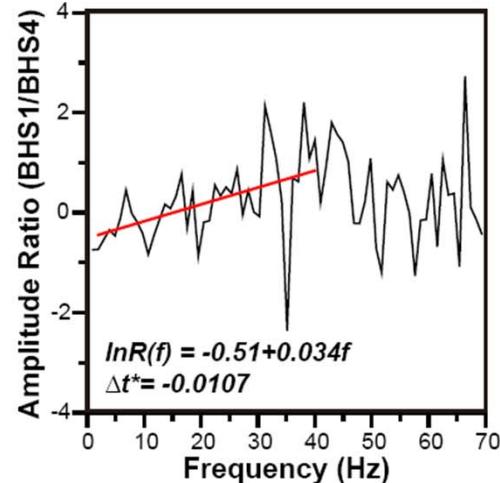
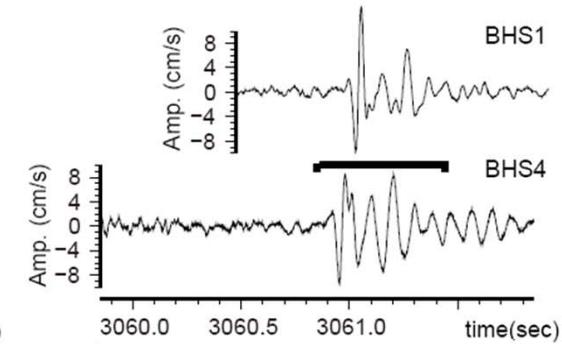
2007/01/30 10:44 Mw 0.46



2007/02/10 19:52 Mw 0.49



2007/02/28 13:50 Mw 0.72



A selection of near-surface attenuation results in borehole ( $\geq 100$  m) studies in California.

Location	Depth Range (m)	$Q_P$	$Q_S$	Rock Type	Authors
Oroville	0-475	—	9	ophiolite	Malin <i>et al.</i> (1988)
Oroville	375-475	—	11	ophiolite	Malin <i>et al.</i> (1988)
Anza	0-150	6.5	9	granite	Aster and Shearer (1991)
Anza	150-300	27	26	granite	Aster and Shearer (1991)
Garner Valley	0-220	—	12	soil, weathered granite, and granite	Archuleta <i>et al.</i> (1992)
Santa Clara Valley	10-35	—	10	Quaternary alluvium	Gibbs <i>et al.</i> (1994)
Santa Clara Valley	40-115	—	15	Quaternary alluvium	Gibbs <i>et al.</i> (1994)
Parkfield	0-200	6-11	8-19	Tertiary sediments	Blakeslee and Malin (1991)
Parkfield	0-300	—	10	Tertiary sediments	Jongmans and Malin (1995)
Parkfield	0-1000	—	37	Tertiary sediments	Jongmans and Malin (1995)
Los Angeles basin	0-420	45	—	Pleistocene and Pliocene sediments	Hauksson <i>et al.</i> (1987)
Los Angeles basin	420-1500	43	25	Pleistocene and Pliocene sediments	Hauksson <i>et al.</i> (1987)
Cajon Pass	700-1500	$36 \pm 11$	$24 \pm 6$	Mesozoic crystalline basement	Abercrombie (1997)

**Table 2.**  $Q$  as a Function of Depth Within the Varian Well:  
From This Study and Jongmans and Malin [1995]

Depth Interval, m	$Q_P$	$Q_S$	Error	$Q_S$ From J&M
0-298	~20	~10	-	8 (7-9)
298-572	-	-	-	8 (7.7-9)
298-938	30	31	25	-
572-938	55	-	30	65 (53-94)
(0 & 23.5) - 938	33	18	30	37 (33-45)

(Abercrombie, 2000)

### Chelungpu fault:

**$Q_S_1$  (945-1110 m): 21-22**

**$Q_P_1$  : 27-35**

**$Q_S_4$  (1110-2000 m): 45**

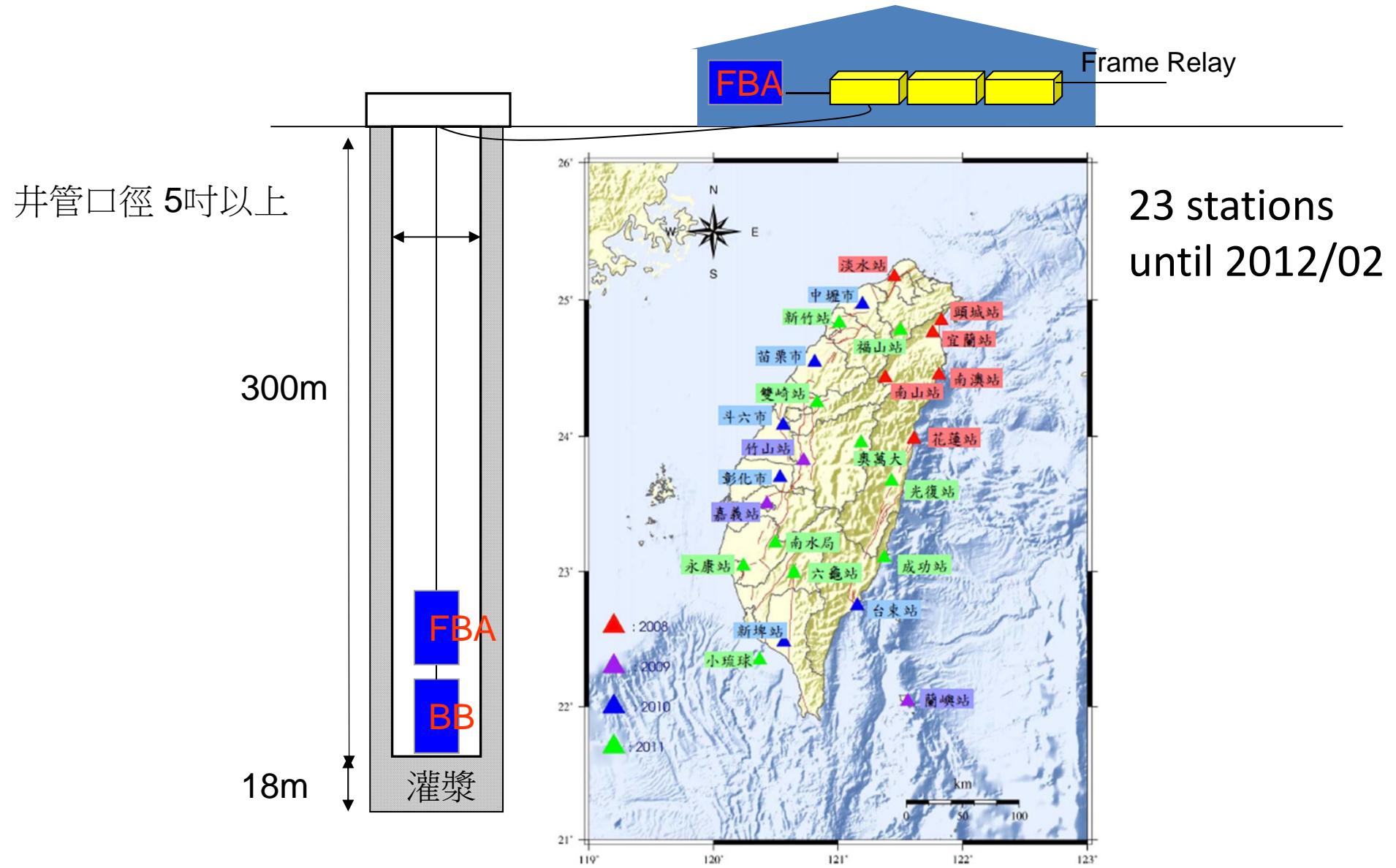
**$Q_P_4$  : 85**

Wang et al. (2012)

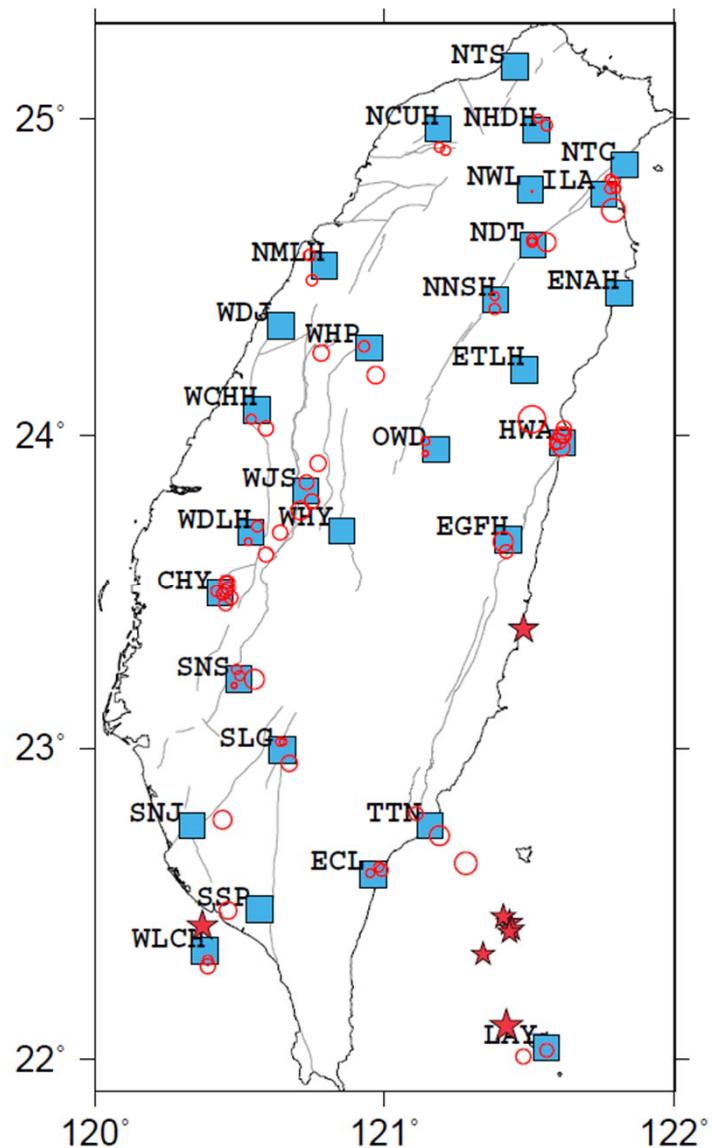
→ The consistency implies that the existence of fluid, fracture and crack may dominate the attenuation feature of the near surface materials around the fault zone rather than the rock type.

# The subsurface attenuation model of Taiwan (depth ~300 m depth)

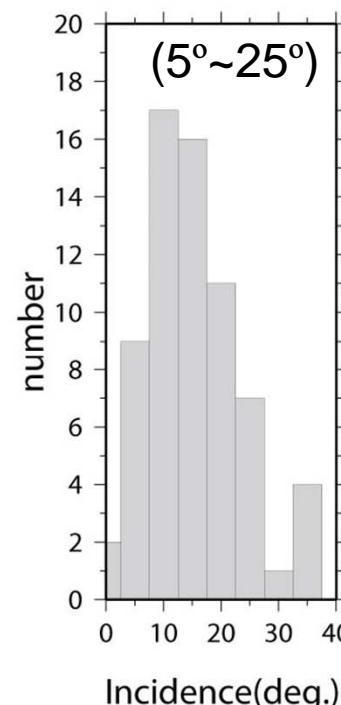
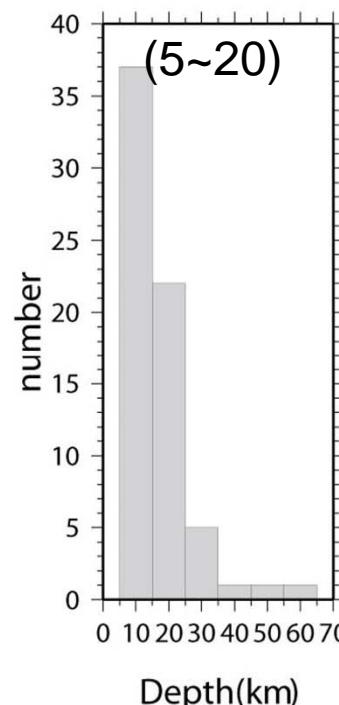
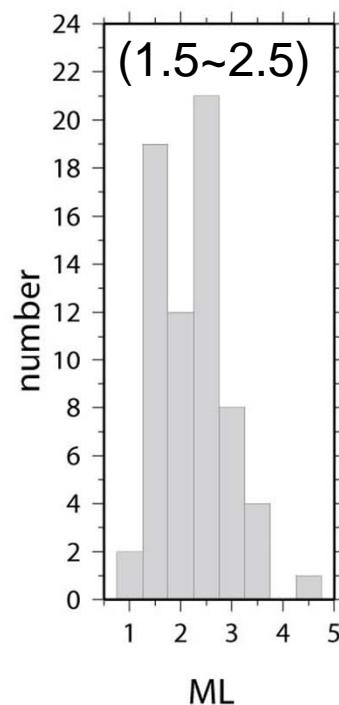
# CWB borehole network

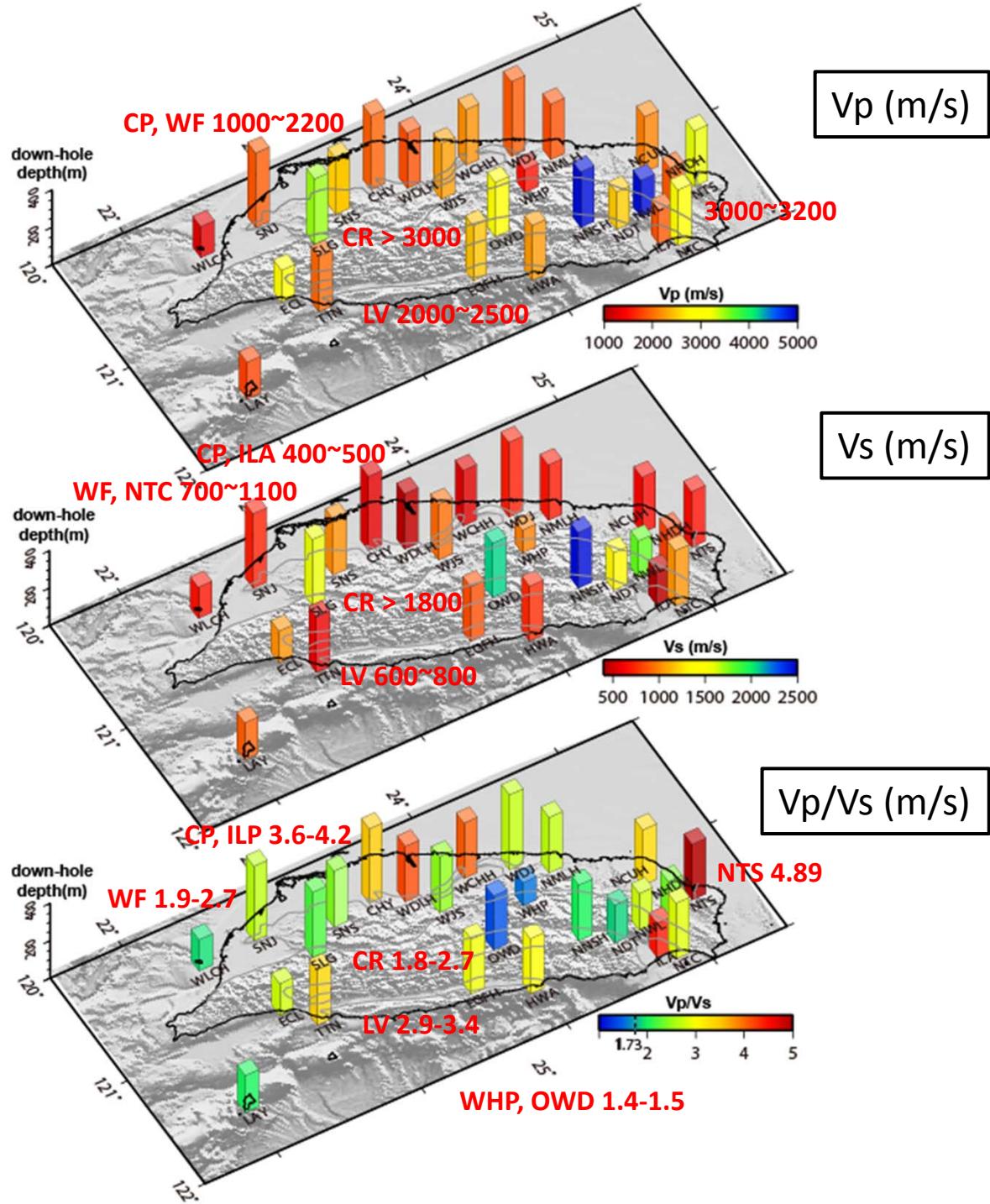
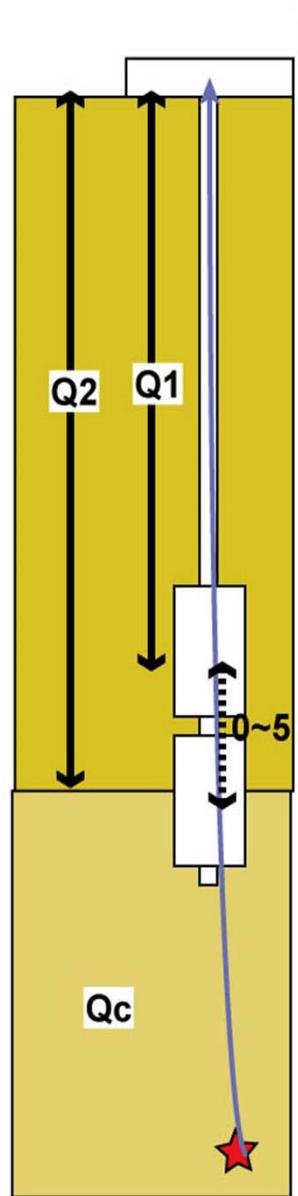


# CWB borehole data

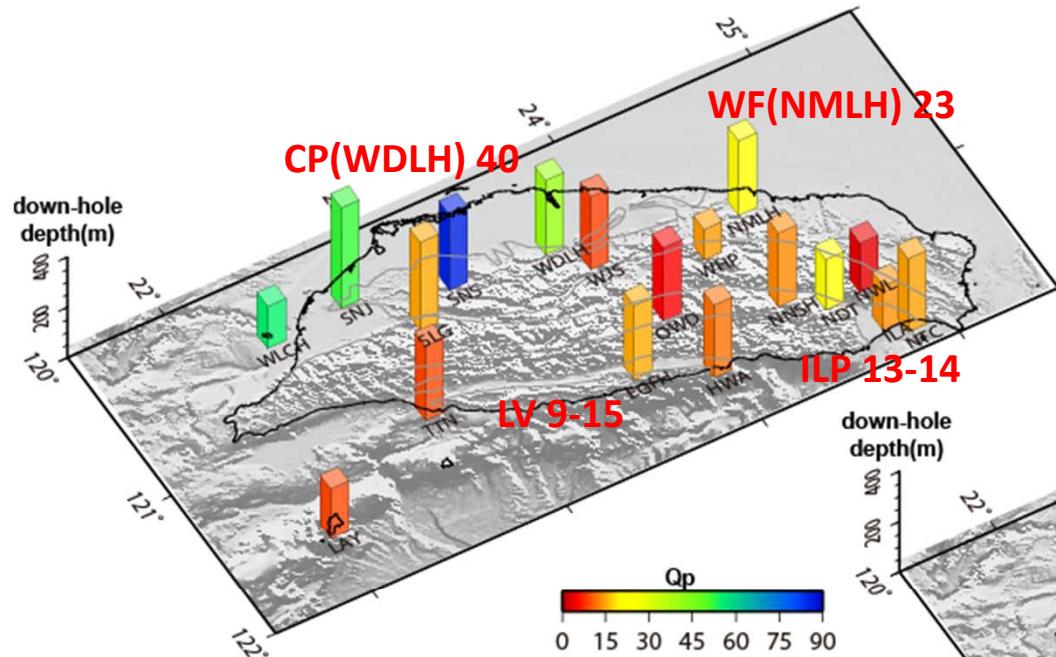


- Data period: 2011/10-2013/05
- high SN ratio and low incidence angle (< 35 deg.)
- **67 events** ( $ML < 4.5$ )
- **8 events** ( $4.0 < ML < 6.0$  ;  $18 \text{ km} < \text{Depth} < 77 \text{ km}$ )

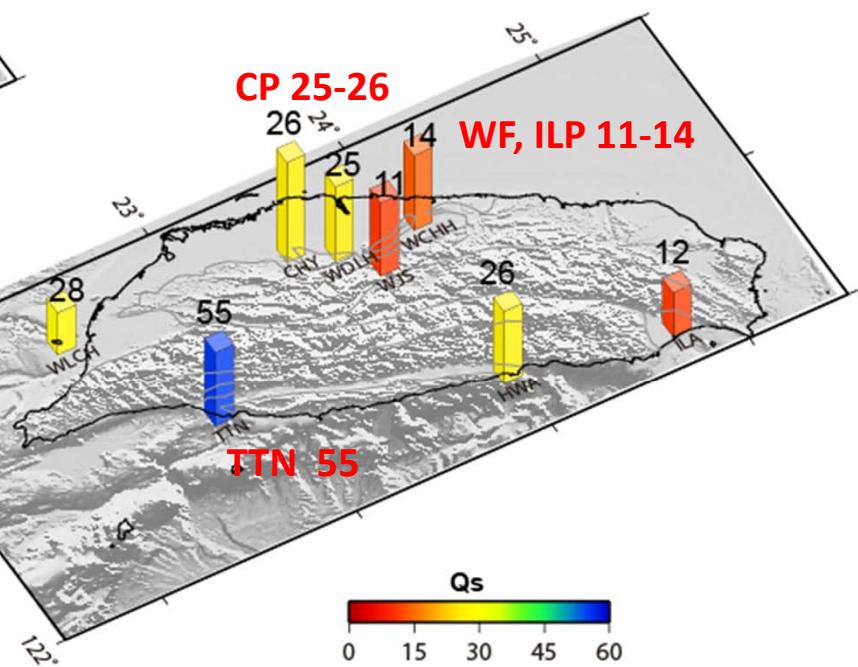




# Q<sub>p</sub>

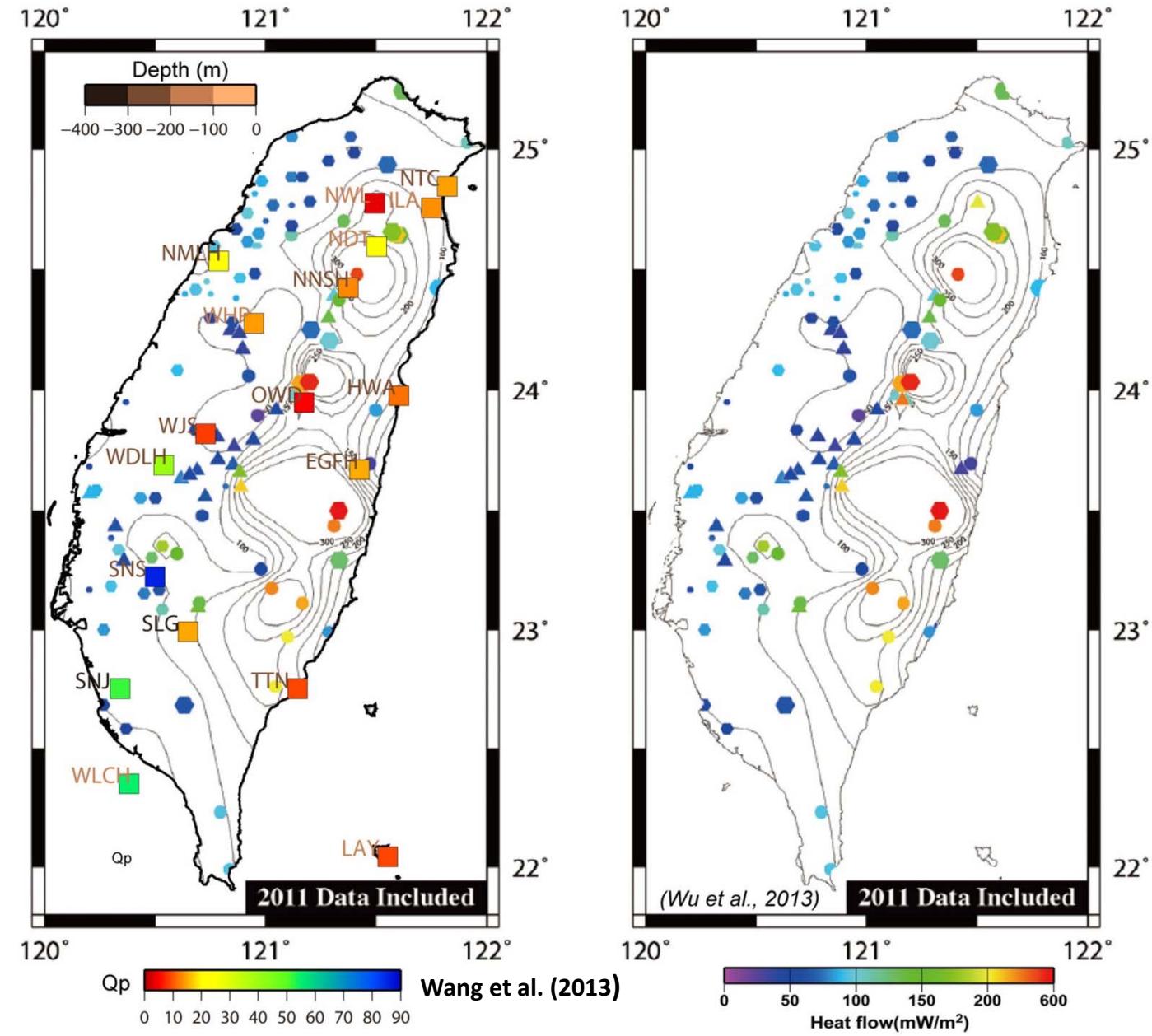


# Q<sub>s</sub>

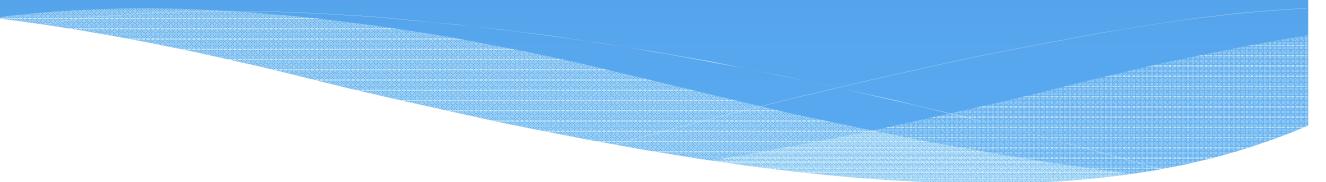


- Q<sub>p</sub> of 18 sites: 0~90 (most sites < 15)
- Maximum Q<sub>p</sub> : 86 (SNS) ;
- Minimum Q<sub>p</sub>: 3.5-4.9 (NWL、OWD)
- CR Q<sub>p</sub>: 5~15 (NDT 24), lower than WF

**Low Q<sub>p</sub> in CR  
~ area of high  
thermal heat flow**

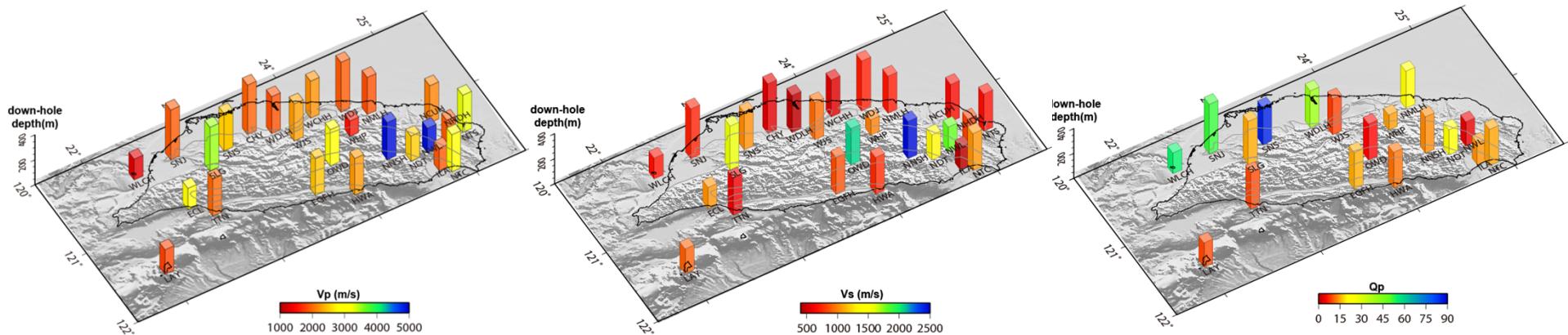


# Attenuation applied in seismic engineering

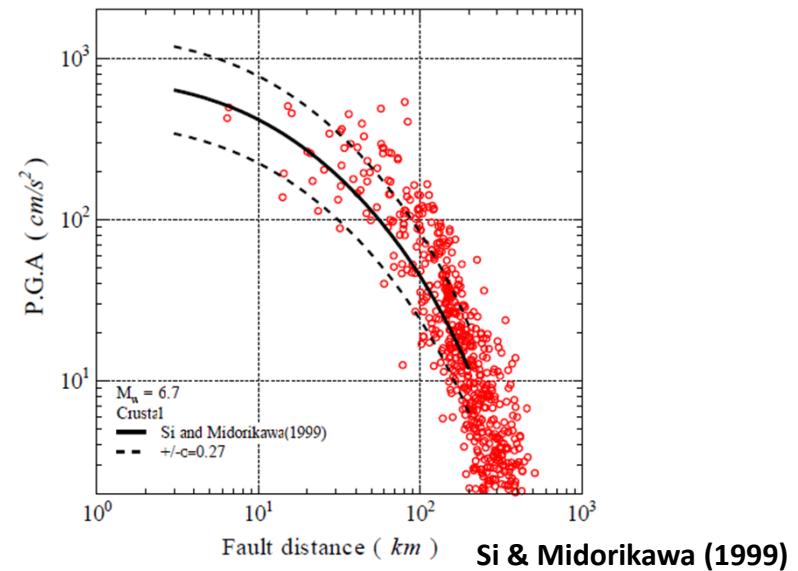
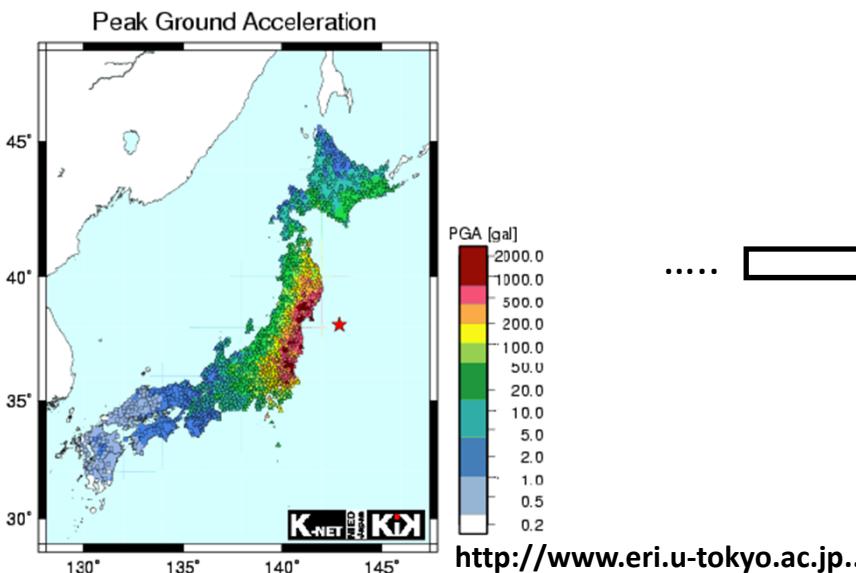


# Strong ground motion prediction

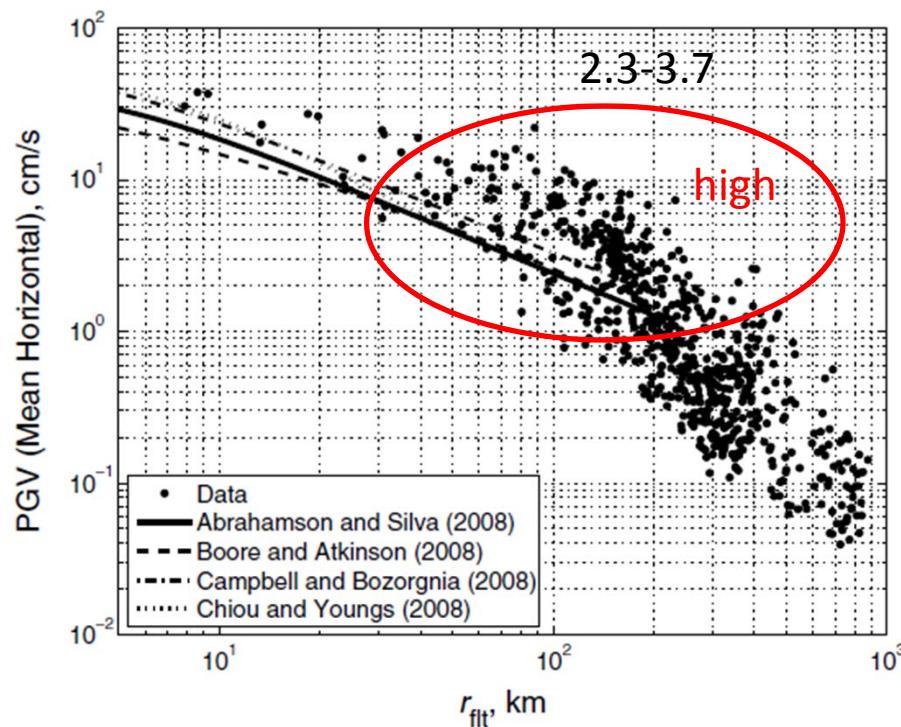
## ① Ground motion simulation



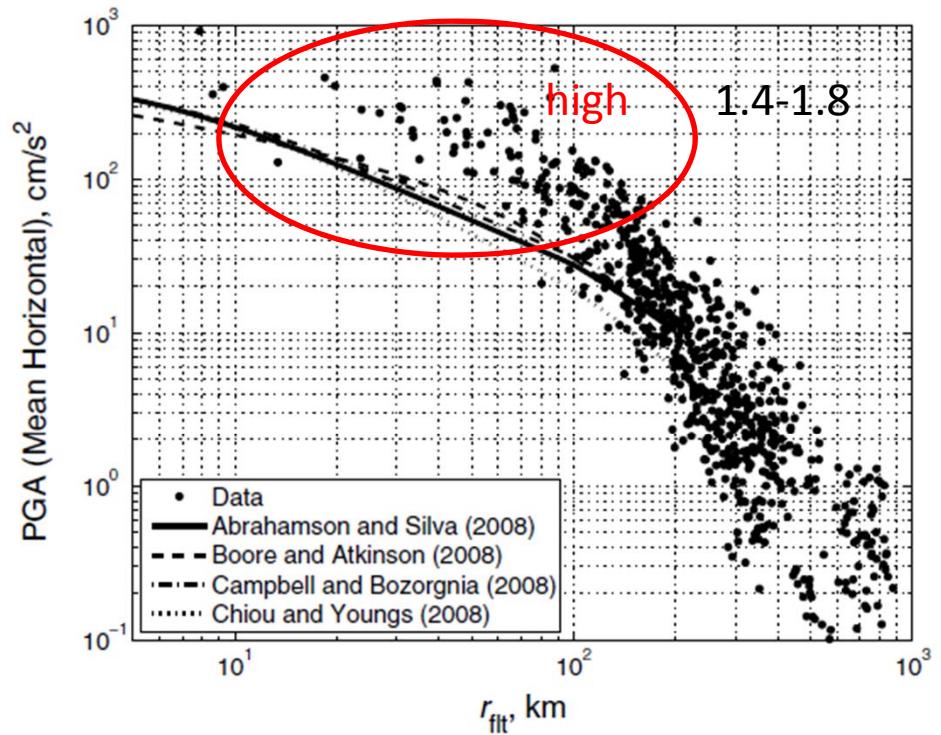
## ② Ground Motion Prediction Equation (GMPE)



# PGA & PGV compared with GMPEs of NGA2008



**Figure 5.** PGV compared with four different GMPEs. Curves assume  $V_{S30} = 400$  m/s, as explained in the text.



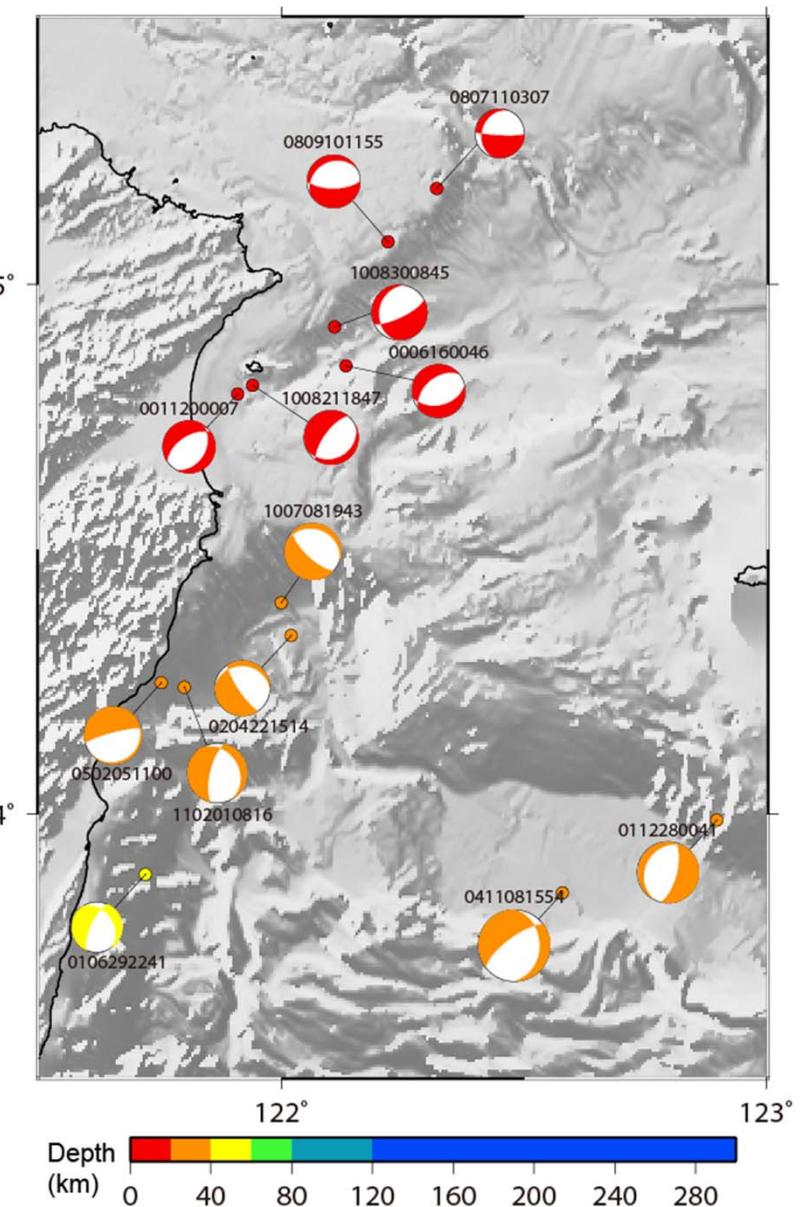
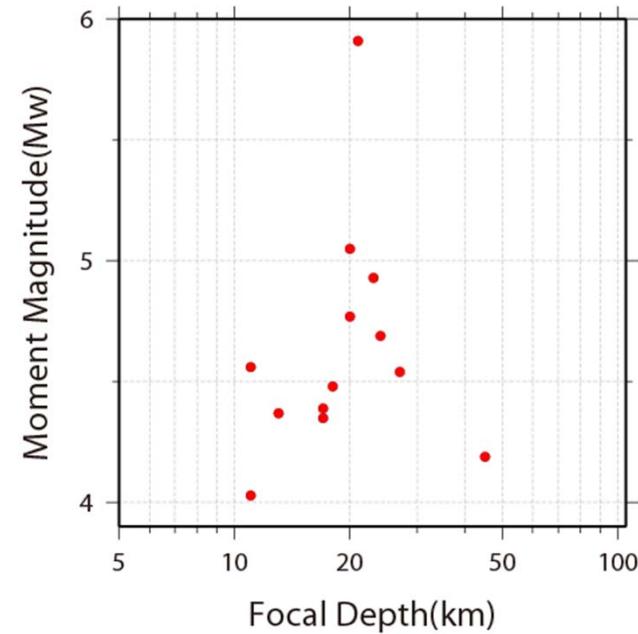
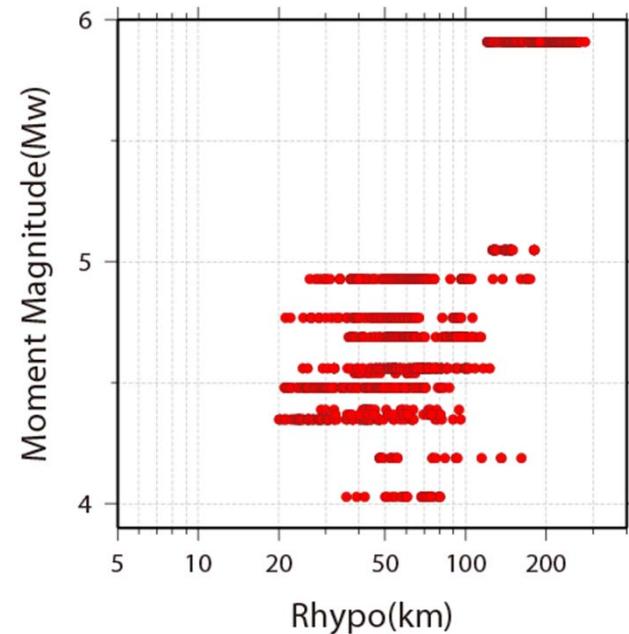
**Figure 4.** PGA, compared with four different GMPEs. Curves assume  $V_{S30} = 400$  m/s, as explained in the text.

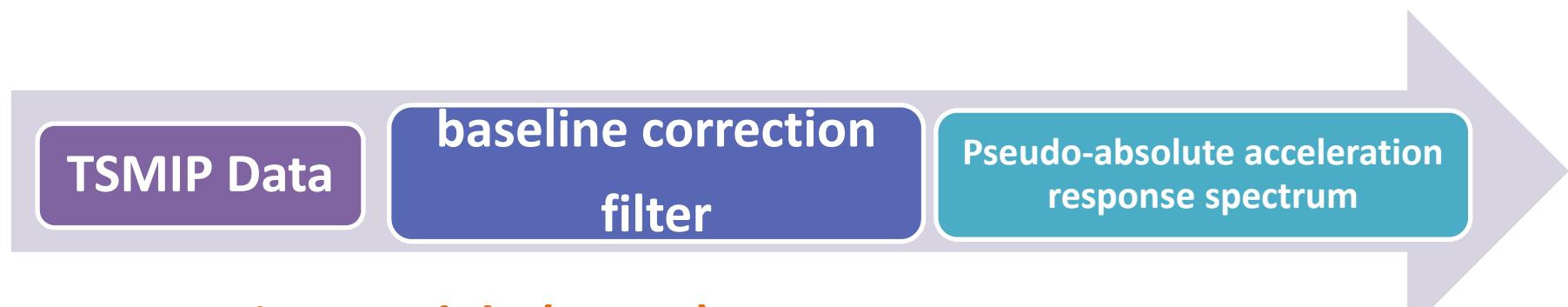
- A different choice of  $V_{S30}$  can not help significantly to reduce the discrepancy.

Anderson et al. (2013)

## Normal faulting events:

**BATS (1995-2013)**  
**Mw>4.0**  
**Rake:-60~-90**  
**recorded by at least 20 station**  
**Total events:13**  
**Total records:1067**





### Attenuation model I (Case1):

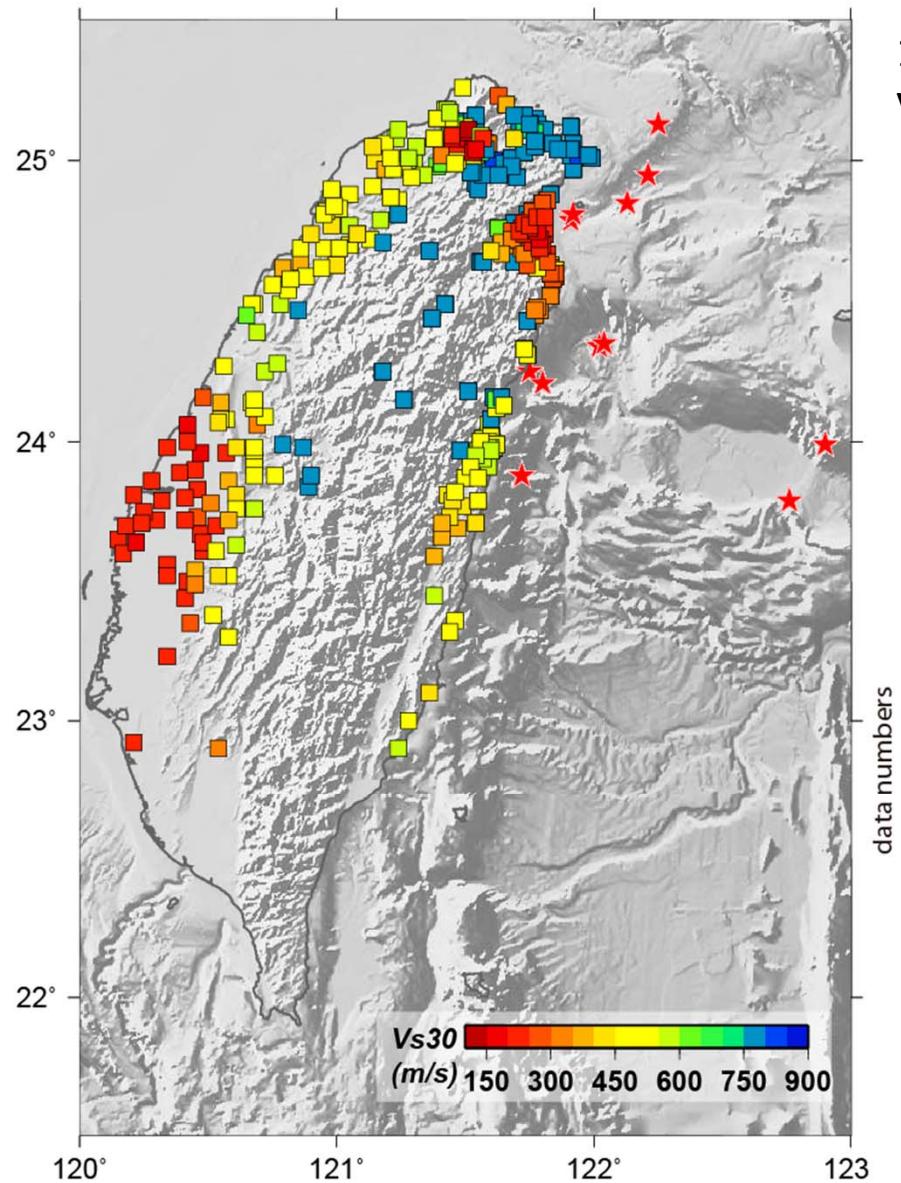
$$\rightarrow \ln(PGA \text{ or } Sa) = C_1 + C_2 Mw + C_3 \ln(R_{hypo} + C_4 e^{C_5 Mw}) + C_6 H_i + C_7 * \ln(Vs_{30}/1130)$$

(Lin 2011, INER report)

### Attenuation model II (Case 3):

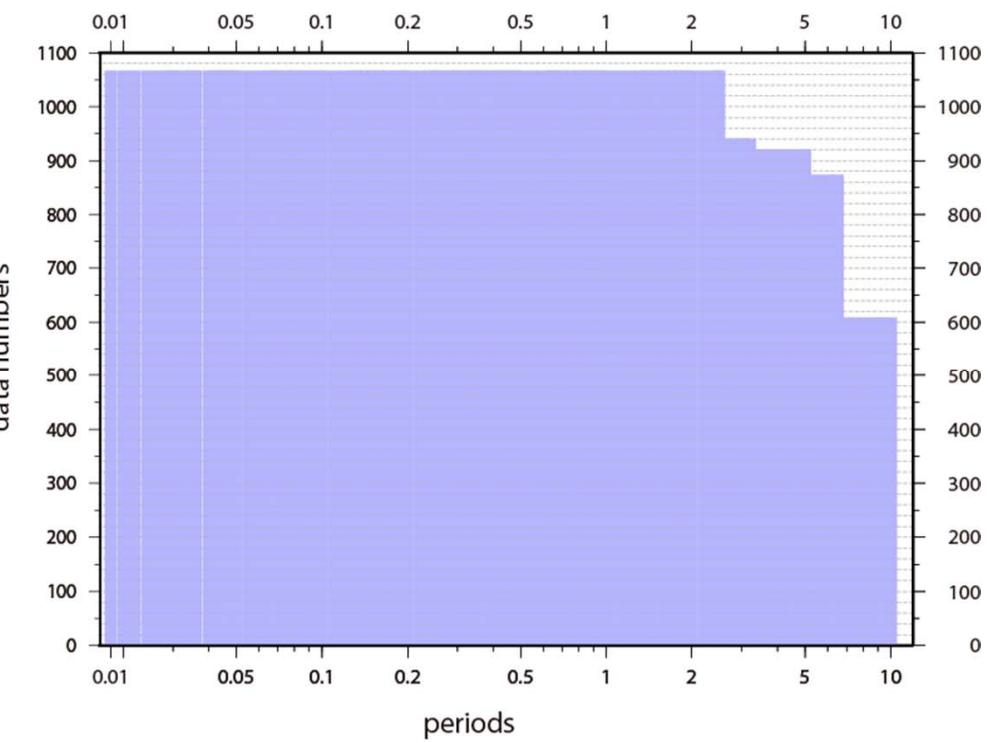
$$\rightarrow \ln(PGA \text{ or } Sa) = C_1 + C_2(Mw - 6.3) + C_3(8.5 - Mw)^2 + (C_4 + C_5(Mw - 6.3))\ln\left(\sqrt{R_{hypo}^2 + (e^H)^2}\right) + C_6 \ln(Vs_{30}/1130)$$

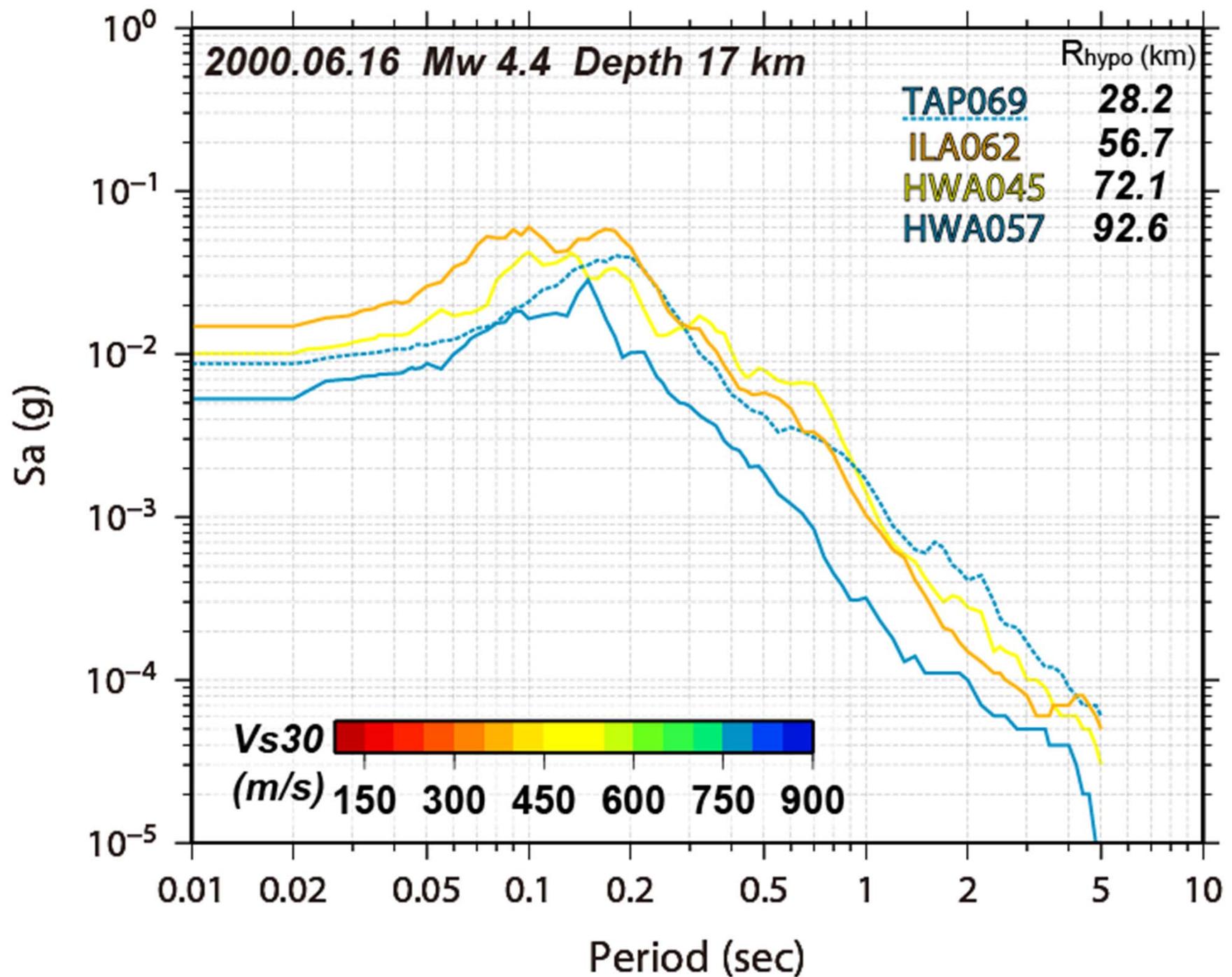
(Lin, 2009)



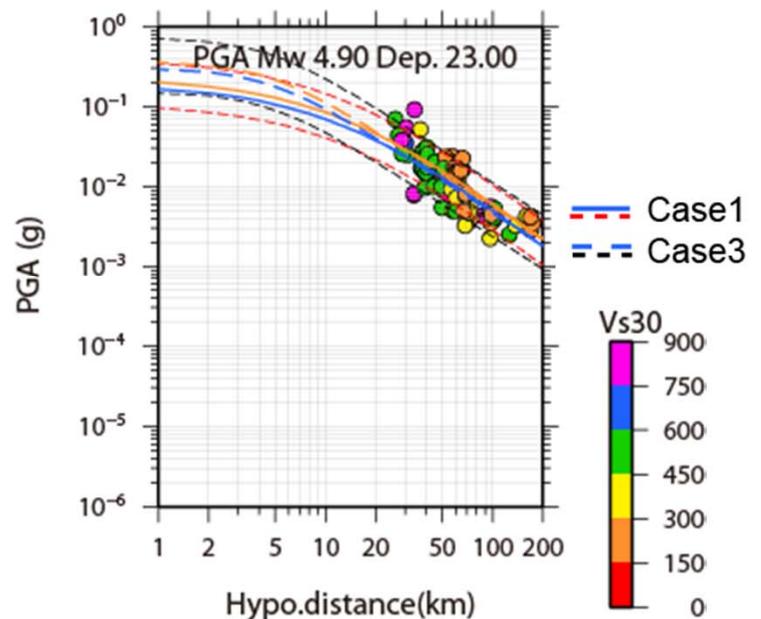
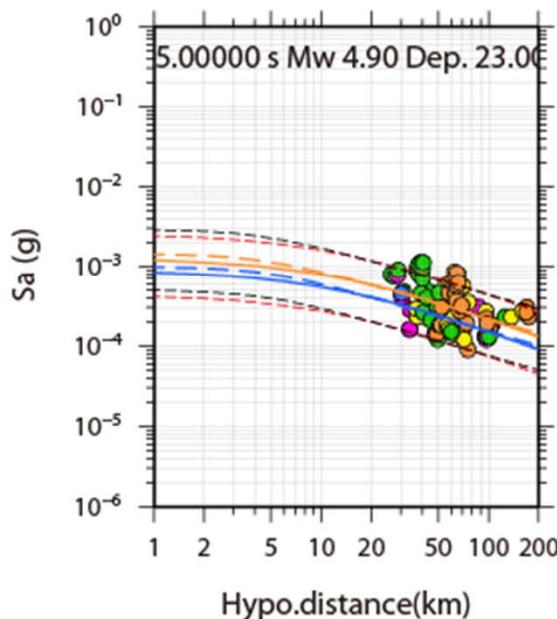
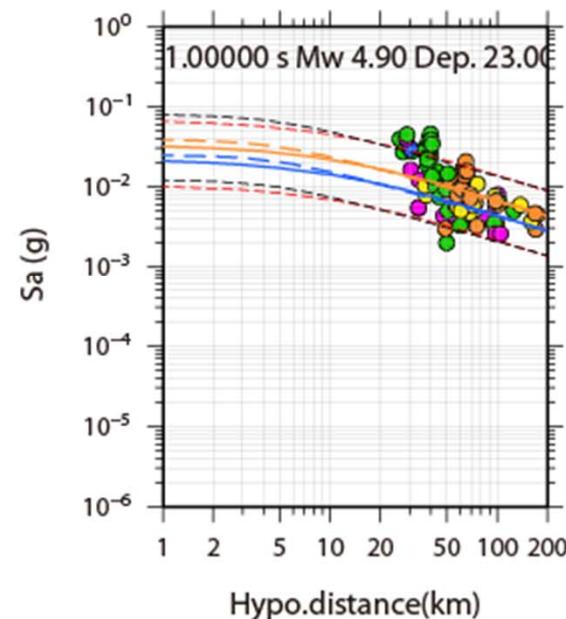
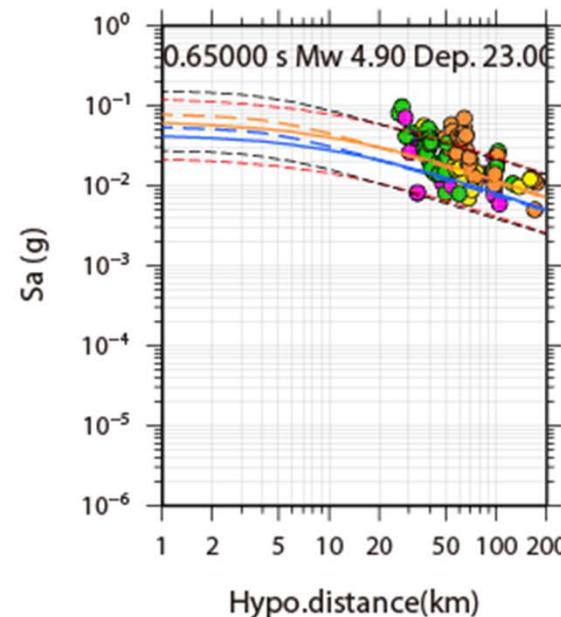
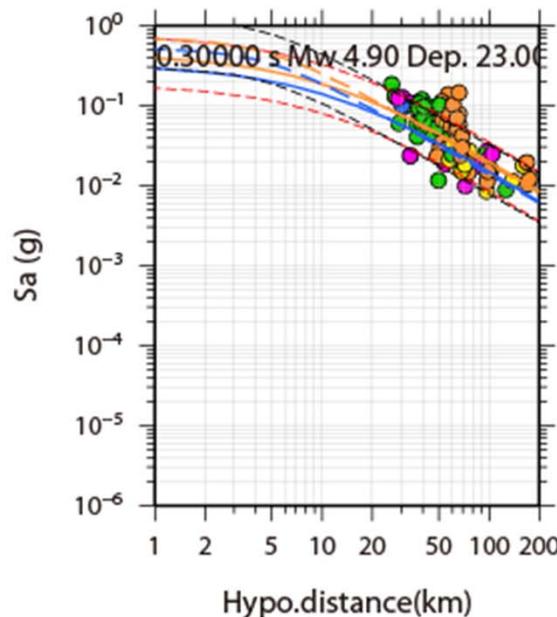
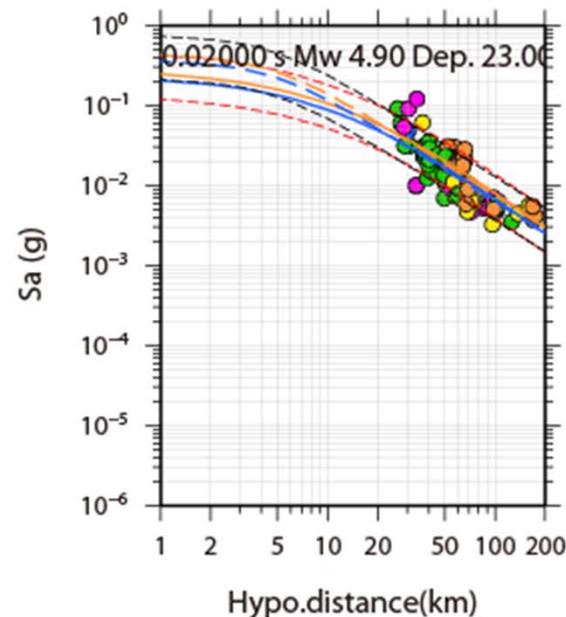
(Vs30 from Lee & Tsai, 2008)

1067 records :  
Vs30 range: 110~835 (m/s)



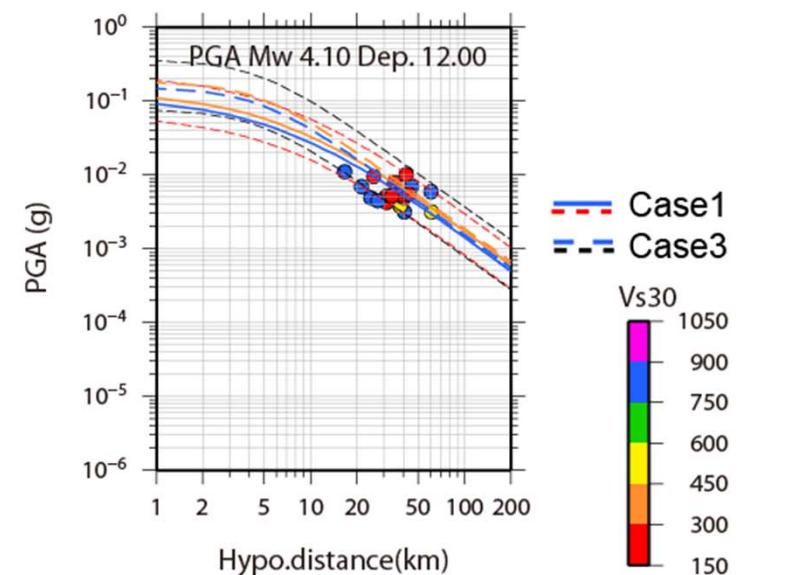
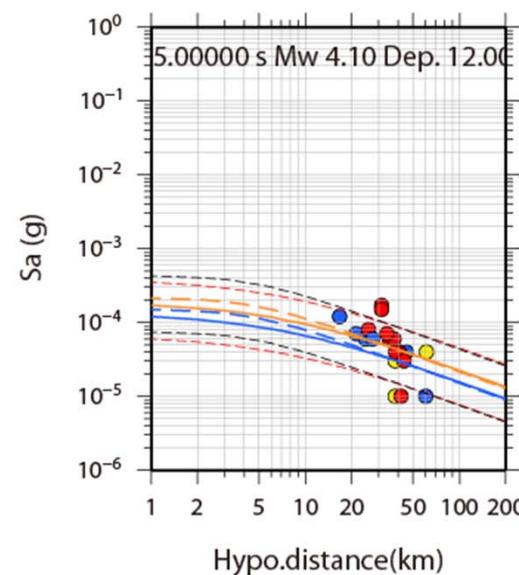
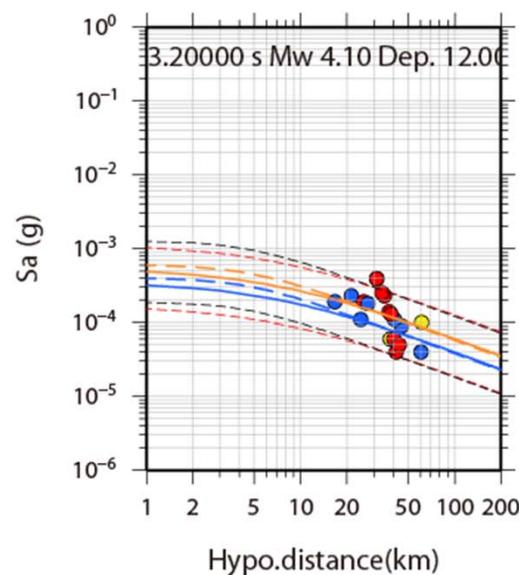
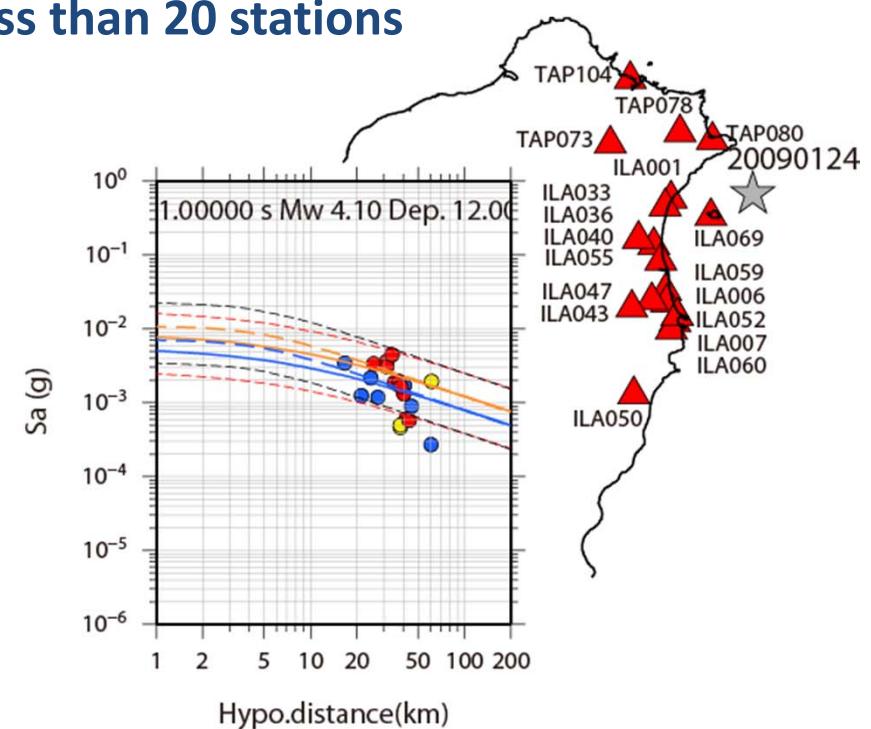
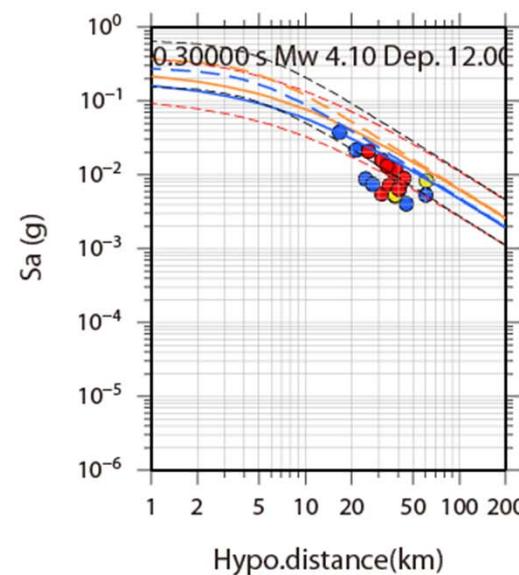
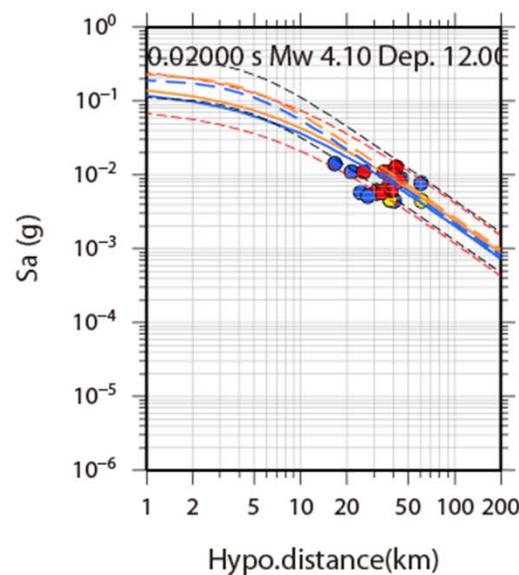


2011.02.01 Discrepancy between Case1 & Case3 : hypocentral distance < 20 km → simulation

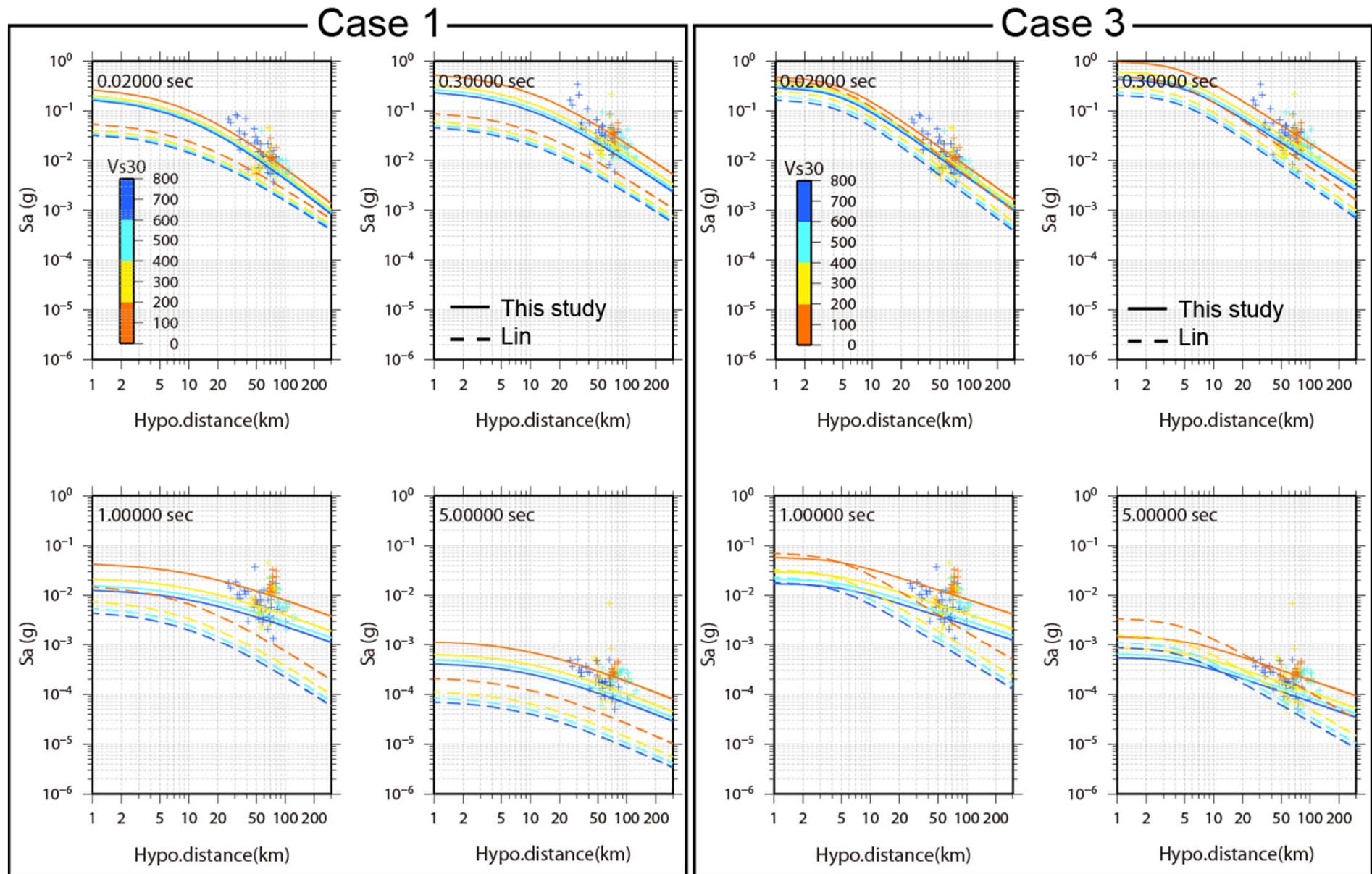


## Comparison with data recorded by less than 20 stations

EQ ID 200901241348



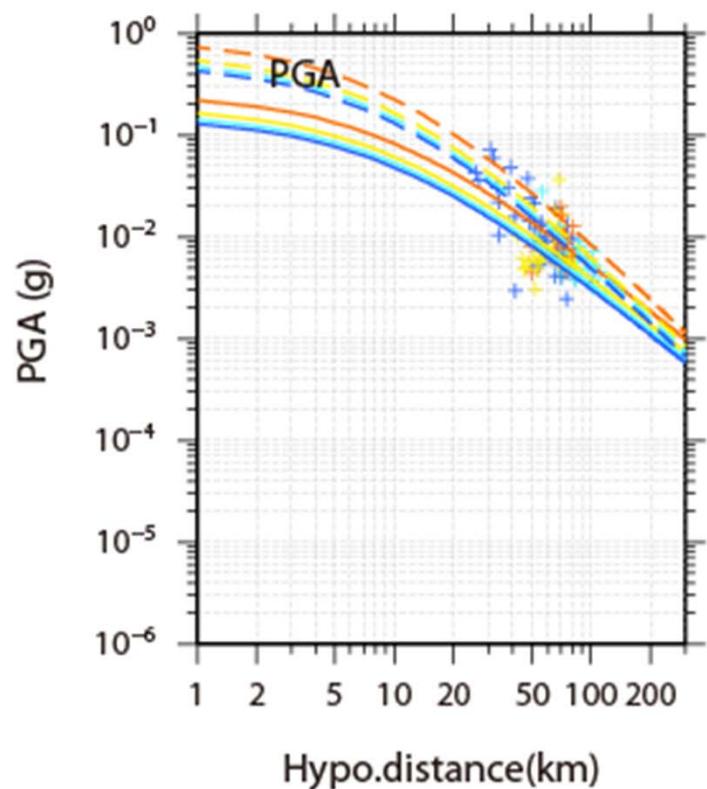
2010.08.30 08:45 Mw 4.6 Dep. 11km



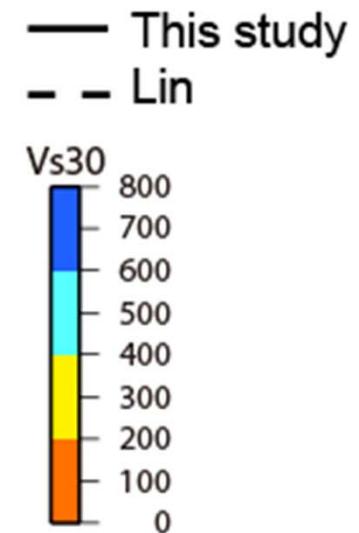
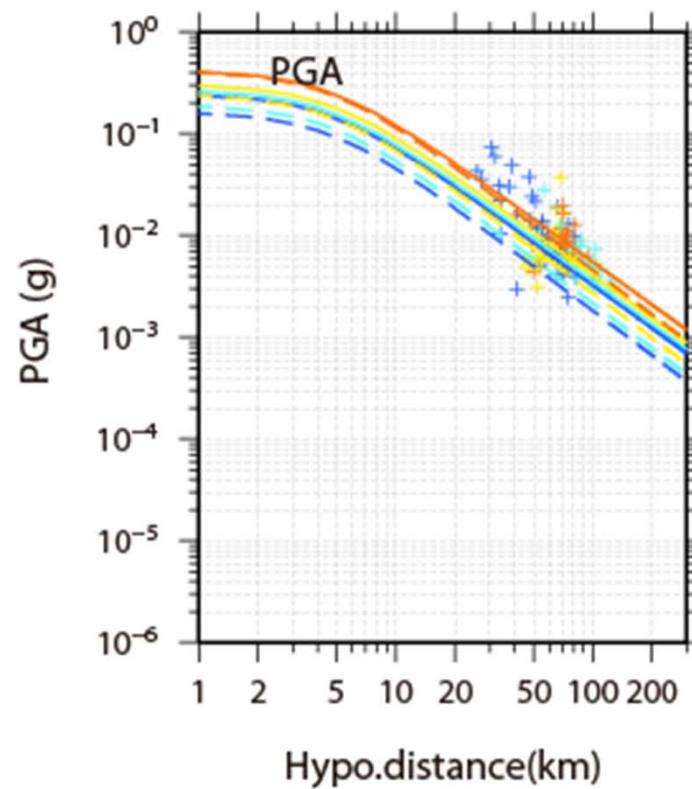
Normal faulting earthquake generates stronger  $S_a$ .

2010.08.30 08:45 Mw 4.6 Dep. 11km

## Case 1



## Case 3



No difference between equations with and without considering fault mechanism.

The new GMPE for PGA do not reveal higher values for normal faulting earthquakes with Mw 4~6.

# summaries

- \* The *spatial variation in Qp-, and Qs-* tomography reflect several prominent tectonic structural features and the structure heterogeneity bounded by the *fault systems*, ex. *Chelungpu Fault, Pingtung Plain*.
- \* The *low Qp and Qs* beneath the *Central Range* coincides well with the observed *aseismic zone*, and imaged *high temperature*. The low Q feature might be related to the high thermal extension resulted from *lower crust exhumation* during collision process.
- \* The significantly *low Qp and low Qs* within the Chelungpu fault zone was attributed to the *existence of fluid, fracture and crack*.
- \* The *high heat flow* area in the Central Range exhibits *low Qp* values of the subsurface Qp model.
- \* The resultant attenuation relationship shows that the normal faulting earthquake generates *stronger Sa* which is not adopted for attenuation equation that usually used in Taiwan. The new GMPE for *PGA do not reveal higher values* for normal faulting earthquakes with Mw 4~6.

FIN

Thank you for your attention~